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Candidate signature			

Level 2 Certificate FURTHER MATHEMATICS

Paper 2 Calculator

Monday 17 June 2019

Afternoon

Time allowed: 2 hours

Materials

For this paper you must have:

- a calculator
- · mathematical instruments.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.
- In all calculations, show clearly how you work out your answer.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 105.
- You may ask for more answer paper, graph paper and tracing paper.
 These must be tagged securely to this answer book.
- The use of a calculator is expected but calculators with a facility for symbolic algebra must **not** be used.

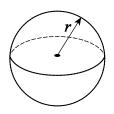
For Exam	iner's Use
Pages	Mark
3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26–27	
28–29	
30	
TOTAL	



Formulae Sheet

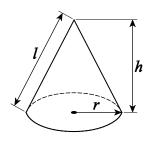
Volume of sphere =
$$\frac{4}{3}\pi r^3$$

Surface area of sphere = $4\pi r^2$



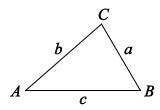
Volume of cone =
$$\frac{1}{3}\pi r^2 h$$

Curved surface area of cone = $\pi r l$



In any triangle ABC

Area of triangle = $\frac{1}{2}ab \sin C$



Sine rule
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$, where $a \ne 0$, are given by $x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$

Trigonometric Identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \qquad \sin^2 \theta + \cos^2 \theta = 1$$

Answer all questions in the spaces provided.

1 (a)
$$a \binom{3}{5} = 4 \binom{2a+3}{b}$$

Work out the values of a and b.

[3 marks]

1 (b)
$$\binom{m-1}{1} \binom{2}{-2} = I$$
 where I is the identity matrix.

Work out the value of m.

[2 marks]

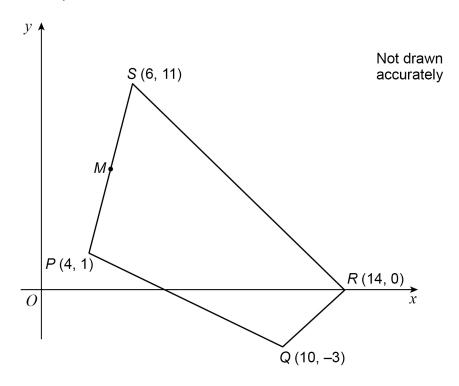
Answer _____

5



2 Here is a sketch of quadrilateral *PQRS*.

M is the midpoint of PS.



Use gradients to show that <i>MR</i> is parallel to <i>PQ</i> .	[3 marks]



3 -2 < a < 0 and -1 < b < 1

Tick the correct box for each statement.

[4 marks]

Sometimes true	Never true
	Sometimes true

$$a^2 < 0$$

$$-1 < b^3 < 1$$

$$\frac{b}{a}$$
 < 0

$$a-b > 0$$







Turn over for the next question

7



4	P is a point on a curve.	
	The curve has gradient function $\frac{x^5 - 17}{10}$	
	The tangent to the curve at <i>P</i> is parallel to the line $3x - 2y = 9$	
	Work out the <i>x</i> -coordinate of <i>P</i> .	
		[4 marks]
	Answer	
	/ triower	

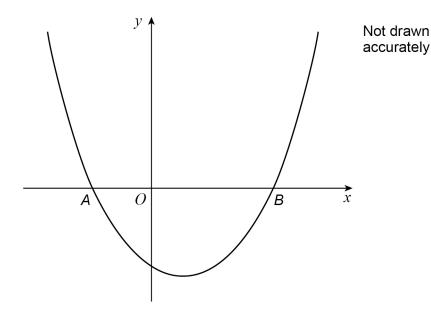
Do not write outside the box

(a)	Write $\sqrt[4]{a \times a^{-9}}$ as an integer power of a .	[2 marks]
	Answer	
(b)	Simplify fully $\frac{(4cd^2)^3}{2cd^4}$	[3 marks]
	Answer	
	Turn over for the next question	



Here is a sketch of the curve y = (2x + 3)(x - 2)6

The curve intersects the *x*-axis at *A* and *B*.



6 (a) Complete the coordinates of A and B.

[2 marks]

Write down the range of values for x for which (2x + 3)(x - 2) < 06 (b)

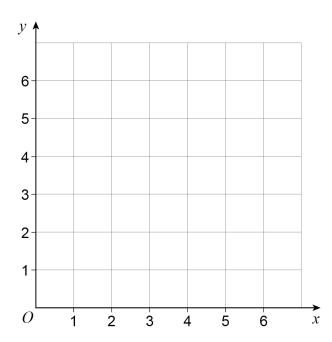
[1 mark]

Answer _____

7 (a) On the grid, sketch a graph for which

the rate of change of y with respect to x is always zero.

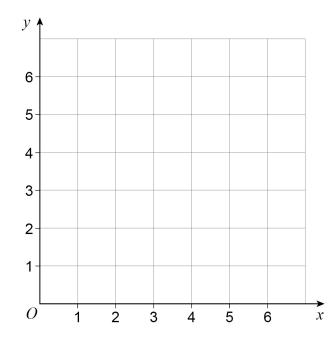
[1 mark]



7 (b) On the grid, sketch a graph for which

the rate of change of y with respect to x is always a positive constant.

[1 mark]



5



8 (a)	A linear sequence has first term $7 + 12\sqrt{5}$	
	The term-to-term rule is	
	add $9-2\sqrt{5}$	
	One term of the sequence is an integer.	
	Work out the value of this integer.	[2 marks]
	Anguer	
	Answer	
8 (b)	The <i>n</i> th term of a different sequence is $\frac{3n^2 - 1}{n^2 + 1}$	
	Work out the sum of the first three terms.	[2 marks]
	Answer	

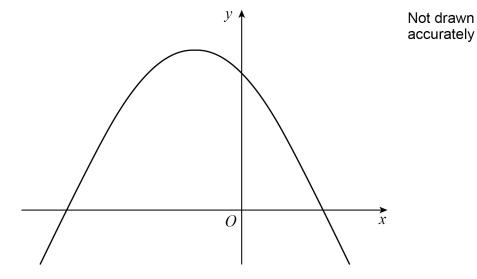
8 (c)	The first four ter	ms of a qu	adratic seq	luence are			
			-3	3	13	27	
	Work out an exp	oression fo	r the <i>n</i> th te	rm.			[3 marks]
		Answer					
		Turi	n over for	the next qu	uestion		



9	Factorise fully $(p+6)^{11} - (p+6)^{10}$	[2 marks]
	Answer	
40 (0)	$f(x) = x^3 - 2$	
10 (a)	The domain of $f(x)$ is $x \le 3$	
	Work out the range of $f(x)$.	[2 marks]
	Answer	
10 (b)	$g(x) = 5 - x^2$	
	The domain of $g(x)$ is $-2 \le x \le 1$	
	Work out the range of $g(x)$.	[2 marks]
	Answer	

Do not write outside the

11 Here is a sketch of a quadratic curve which has a maximum point at (-2, 5)



What is the equation of the normal to the curve at the maximum point? Circle your answer.

[1 mark]

$$x = -2$$

$$y = 5$$

$$x = 5$$

$$x = -2$$
 $y = 5$ $x = 5$ $y = -2$

Turn over for the next question

	e diagram shows a solid hemisphere.	
	The diameter is 12 <i>a</i> cm	
Т	The volume is $486\pi~{ m cm}^3$	
	\leftarrow 12 $a \text{ cm} \longrightarrow$	
Wor.	rk out the value of a .	
VVOI	in out the value of u.	[3 m
	Answer	



Do not write outside the

Simplify fully $\frac{x-x^3}{2x+2x^2}$

You **must** show your working.

[4 marks]

Answer

Turn over for the next question

7



4	Here is a triangle. $\frac{b \text{ cm}}{a \text{ cm}}$	Not drawn accurately	
	Use the cosine rule to work out the ratio b^2 : a^2		[3 marks]
	Answer : :		



Rearrange $m = \frac{2p+1}{p} + \frac{p+5}{3p}$ to make p the s	[4 mark
	Į
Anguer	
Answer	
Allswei	
Answei	
The curve $y = 2\sqrt{x-a} + 5$ passes through the	
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can be written in the form	(x + a)(x + b)	where a and b are positive	e integers I



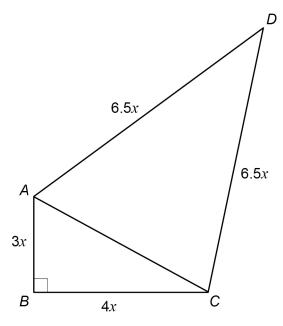
Answer	
Answer	

8



- 19 ABC is a right-angled triangle.
 - ACD is an isosceles triangle.

All dimensions are in centimetres.



Not drawn accurately

19 (a)	Show that	AC = 5x
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	[1	mark]
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	2	

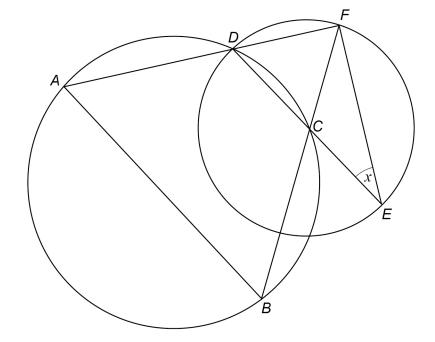
(b)	Work out an expression, in cm ² , for the area of quadrilateral <i>ABCD</i> .	
	Give your answer in the form px^2 where p is an integer.	[5 marks]
	Answer cm ²	
	Turn over for the next question	



- **20** A, B, C and D are points on a circle.
 - ${\it D}, {\it E}$ and ${\it F}$ are points on a different circle, centre ${\it C}.$

DCE, ADF and BCF are straight lines.

angle DEF = x



Not drawn accurately

[3 marks	angle <i>BAD</i> = 2x	Prove that	20 (a)



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20 (b)	In the case when AB is parallel to DE, work out the size of angle	x. [2 marks]
	Answerde	egrees
	Turn over for the next question	

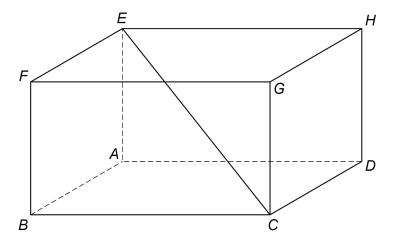


21 ABCDEFGH is a cuboid.

$$BC = 15 \text{ cm}$$

Answer

$$DH = 8 \text{ cm}$$



Work out the size of the angle between the line CE and the plane CDHG.

Γ4	m	ar	ksl
ъ.	•••	ч.	



degrees

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22 (a) Show that $\frac{2\sin^2 x - 1 + \cos^2 x}{\sin x \cos x}$ is equivalent to $\tan x$

[3 marks]

22 (b) Hence solve $\frac{2\sin^2 x - 1 + \cos^2 x}{\sin x \cos x} = -1$ for $0^{\circ} \le x \le 360^{\circ}$

[2 marks]

Answer

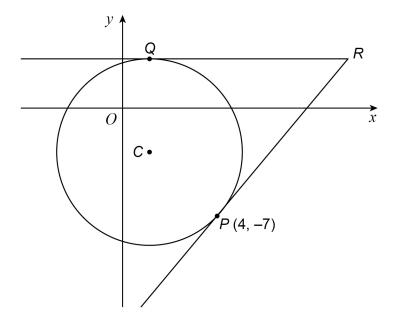
9



A circle has centre C and equation $(x-1)^2 + (y+3)^2 = 25$ P (4, -7) and Q are points on the circle.

The tangent at Q is parallel to the *x*-axis.

The tangents at *P* and *Q* intersect at point *R*.



Not drawn accurately

23 (a) Write down the coordinates of *C*.

[1 mark]

Answer ____

23	(b)	Show that the equation of the tangent at Q is	y = 2 [1 mark]	outs k
23	(c)	Work out the <i>x</i> -coordinate of <i>R</i> .		
23	(6)	Work out the x-coordinate of K.	[4 marks]	
		Answer		
				6



24	Show that the curve	$y = \frac{3}{5}x^5 + x^4$	has exactly two stationary points.	
		Ü		[4 marks]
	_			
25	$f(x) = x^3 - 10x - c$ v	where c is a posit	ive integer.	
	(x + c) is a factor of $f(x)$	<i>:</i>).		
	Use the factor theoren	n to work out the	value of c .	[3 marke]
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			value of c.	[3 marks]
				[3 marks]
				[3 marks]
				[3 marks]



26	f(x) is a function with domain	all values of x .	
	$f(x) = \sqrt{x^2 + 6x - a}$	where a is a constant.	
	Work out the possible values o	f <i>a</i> .	
	Give your answer as an inequa	ality.	[4 marks]
	Answer		

Turn over for the next question

11

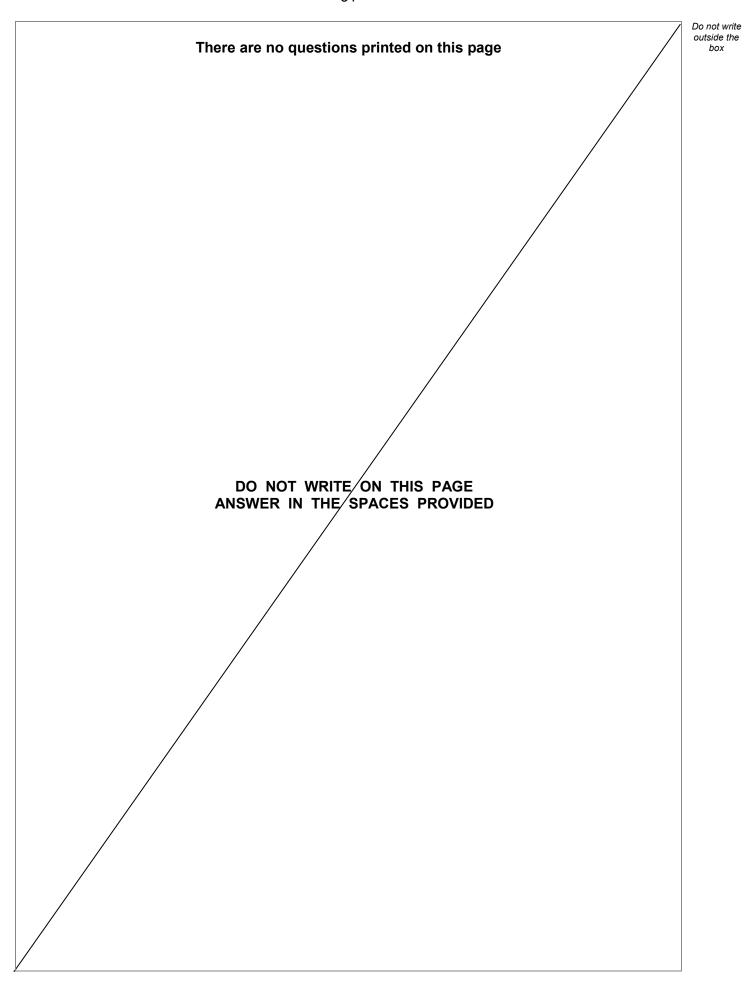


27	The curve	y = f(x)	has	$\frac{dy}{dx} = (x+2)^6 + (x+2)^4$	
	The curve ha	s exactly o	ne static	onary point at P where $x = -2$	
	Use the expr	ession for	$\frac{dy}{dx}$ to sh	how that <i>P</i> is a point of inflection.	
					[3 marks]

END OF QUESTIONS

3







Question number	Additional page, if required. Write the question numbers in the left-hand margin.



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