## 8.5) Binomial estimation

Worked example	Your turn
a) Find the first four terms of the binomial expansion, in ascending powers of $x$ , of $\left(1+\frac{x}{2}\right)^{10}$	a) Find the first four terms of the binomial expansion, in ascending powers of $x$ , of $\left(1+\frac{x}{4}\right)^8$
b) Use your expansion to estimate the value of 1.052 <sup>10</sup> , giving your answer to 4 decimal places	b) Use your expansion to estimate the value of $1.025^8$ , giving your answer to 4 decimal places a) $1 + 2x + \frac{7}{4}x^2 + \frac{7}{8}x^3 + \cdots$ b) $1.2184$ (4 dp)

Worked example	Your turn
a) Find the first four terms of the binomial expansion, in ascending powers of $x$ , of $\left(1-\frac{x}{2}\right)^8$ b) Use your expansion to estimate the value of $0.957^8$ , giving your answer to 4 decimal places	a) Find the first four terms of the binomial expansion, in ascending powers of $x$ , of $\left(1-\frac{x}{4}\right)^{10}$ b) Use your expansion to estimate the value of $0.975^{10}$ , giving your answer to 4 decimal places a) $1-\frac{5}{2}x+\frac{45}{16}x^2\frac{15}{8}x^3+\cdots$ b) 0.7763 (4 dp)

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Worked example	Your turn
a) Find the first three terms of the binomial expansion, in ascending powers of $x$ , of $\left(5 - \frac{x}{7}\right)^6$ b) Use your expansion to estimate the value of 4.996 <sup>9</sup> , giving your answer to 4 significant figures	a) Find the first three terms of the binomial expansion, in ascending powers of $x$ , of $\left(7 - \frac{x}{5}\right)^9$ b) Use your expansion to estimate the value of 6.991 <sup>8</sup> , giving your answer to 4 significant figures a) 40353607 $-\frac{51883209}{5}x + \frac{29647548}{25}x^2 + \cdots$
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Worked example	Your turn
a) Find the first three terms of the binomial expansion, in ascending powers of $x$ , of $\left(1-\frac{x}{3}\right)^8$ b) Use your expansion to estimate the value of 0.96 <sup>8</sup> , giving your answer to 5 decimal places	a) Find the first four terms of the binomial expansion, in ascending powers of $x$ , of $\left(1-\frac{x}{4}\right)^8$ b) Use your expansion to estimate the value of $0.96^8$ , giving your answer to 5 decimal places a) $1-2x+\frac{7}{4}x^2-\frac{7}{8}x^3+\cdots$ b) 0.72122