

8.3) The binomial expansion

Worked example

Use the binomial theorem to find the expansion of $(2 - 3x)^5$

Your turn

Use the binomial theorem to find the expansion of $(3 - 2x)^5$

$$243 - 810x + 1080x^2 - 720x^3 + 240x^4 - 32x^5$$

Worked example

Find the first four terms in ascending powers of x in the binomial expansion of $(1 + 3x)^{11}$

Your turn

Find the first four terms in ascending powers of x in the binomial expansion of $(1 + 2x)^{10}$

$$1 + 20x + 180x^2 + 960x^3 + \dots$$

Worked example

Find the first four terms in ascending powers of x in the binomial expansion of

$$\left(6 - \frac{1}{3}x\right)^{10}$$

Your turn

Find the first four terms in ascending powers of x in the binomial expansion of

$$\left(10 - \frac{1}{2}x\right)^6$$

$$1000000 - 300000x + 37500x^2 - 2500x^3 + \dots$$

Worked example

Find the first 3 terms in the expansion of $\left(3 - \frac{1}{2}x\right)^5$, in ascending powers of x .

Your turn

Find the first 3 terms in the expansion of $\left(2 - \frac{1}{3}x\right)^7$, in ascending powers of x .

$$128 - \frac{448}{3}x + \frac{224}{3}x^2 + \dots$$

Worked example

Find the binomial expansion of $\left(x + \frac{1}{x}\right)^7$ giving each term in its simplest form

Your turn

Find the binomial expansion of $\left(x + \frac{1}{x}\right)^5$ giving each term in its simplest form

$$x^5 + 5x^3 + 10x + \frac{10}{x} + \frac{5}{x^3} + \frac{1}{x^5}$$