

## 7.2) Modelling with statics

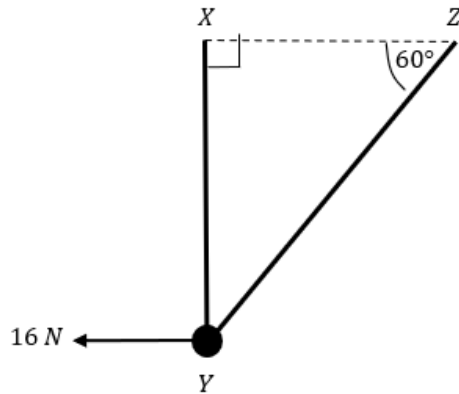
## Worked example

A smooth bead  $Y$  is threaded on a light inextensible string. The ends of the string are attached to two fixed points,  $X$  and  $Z$ , on the same horizontal level.

The bead is held in equilibrium by a horizontal force of magnitude  $16\text{ N}$  acting parallel to  $ZX$ .

The bead  $Y$  is vertically below  $X$  and  $\angle XZY = 60^\circ$  as shown in the diagram.

Find the tension in the string and the weight of the bead.



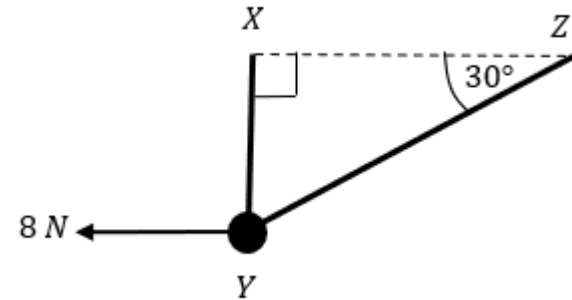
## Your turn

A smooth bead  $Y$  is threaded on a light inextensible string. The ends of the string are attached to two fixed points,  $X$  and  $Z$ , on the same horizontal level.

The bead is held in equilibrium by a horizontal force of magnitude  $8\text{ N}$  acting parallel to  $ZX$ .

The bead  $Y$  is vertically below  $X$  and  $\angle XZY = 30^\circ$  as shown in the diagram.

Find the tension in the string and the weight of the bead.



$$\text{Tension} = 9.24\text{ N (3 sf)}$$

$$\text{Weight} = 13.9\text{ N (3 sf)}$$

## Worked example

A mass of 6kg rests on the surface of a smooth plane which is inclined at an angle of  $30^\circ$  to the horizontal. The mass is attached to a cable which passes up the plane along the line of greatest slope and then passes over a smooth pulley at the top of the plane.

The cable carries a mass of 2kg freely suspended at the other end.

The masses are modelled as particles, and the cable as a light inextensible string.

There is a force of  $P$  N acting horizontally on the 6kg mass and the system is in equilibrium.

Calculate:

- (a) the magnitude of  $P$
- (b) the normal reaction between the mass and the plane
- (c) State how you have used the assumption that the pulley is smooth in your calculations.

## Your turn

A mass of 3kg rests on the surface of a smooth plane which is inclined at an angle of  $45^\circ$  to the horizontal.

The mass is attached to a cable which passes up the plane along the line of greatest slope and then passes over a smooth pulley at the top of the plane.

The cable carries a mass of 1kg freely suspended at the other end.

The masses are modelled as particles, and the cable as a light inextensible string.

There is a force of  $P$  N acting horizontally on the 3kg mass and the system is in equilibrium.

Calculate:

- (a) the magnitude of  $P$
- (b) the normal reaction between the mass and the plane

a)  $P = 16$  (2 sf)

b)  $32$  (2 sf)

## Worked example

A particle of weight  $4\text{ N}$  is attached at  $C$  to the ends of two light inextensible strings  $AC$  and  $BC$ .

The other ends,  $A$  and  $B$ , are attached to a fixed horizontal ceiling. The particle hangs at rest in equilibrium, with the strings in a vertical plane. The string  $AC$  is inclined at  $45^\circ$  to the horizontal and the string  $BC$  is inclined at  $15^\circ$  to the horizontal. Find:

- The tension in the string  $AC$
- The tension in the string  $BC$

## Your turn

A particle of weight  $8\text{ N}$  is attached at  $C$  to the ends of two light inextensible strings  $AC$  and  $BC$ .

The other ends,  $A$  and  $B$ , are attached to a fixed horizontal ceiling. The particle hangs at rest in equilibrium, with the strings in a vertical plane. The string  $AC$  is inclined at  $35^\circ$  to the horizontal and the string  $BC$  is inclined at  $25^\circ$  to the horizontal. Find:

- The tension in the string  $AC$
- The tension in the string  $BC$

a)  $8.4\text{ N}$  (2 sf)

b)  $7.6\text{ N}$  (2 sf)