

7.2) Using the angle addition formulae

Worked example

Using the trigonometric angle addition formulae find:

$$\sin 75^\circ$$

$$\tan 75^\circ$$

Your turn

Using the trigonometric angle addition formulae find:

$$\cos 75^\circ$$
$$\frac{\sqrt{6} - \sqrt{2}}{4}$$

Worked example

Using the trigonometric angle addition formulae find:

$$\sin 15^\circ$$

$$\tan 15^\circ$$

Your turn

Using the trigonometric angle addition formulae find:

$$\cos 15^\circ$$
$$\frac{\sqrt{6} + \sqrt{2}}{4}$$

Worked example

Using the trigonometric angle addition formulae evaluate:

$$\sin 30^\circ \cos 60^\circ + \cos 30^\circ \sin 60^\circ$$

$$\cos 20^\circ \cos 25^\circ - \sin 20^\circ \sin 25^\circ$$

$$\frac{\tan \frac{\pi}{18} + \tan \frac{\pi}{9}}{1 - \tan \frac{\pi}{18} \tan \frac{\pi}{9}}$$

Your turn

Using the trigonometric angle addition formulae evaluate:

$$\sin 60^\circ \cos 30^\circ - \cos 60^\circ \sin 30^\circ$$

$$\sin 30^\circ = \frac{1}{2}$$

$$\cos 70^\circ \cos 25^\circ + \sin 70^\circ \sin 25^\circ$$

$$\cos 45^\circ = \frac{\sqrt{2}}{2}$$

$$\frac{\tan \frac{13\pi}{36} - \tan \frac{\pi}{9}}{1 + \tan \frac{13\pi}{36} \tan \frac{\pi}{9}}$$

$$\tan \frac{\pi}{4} = 1$$

Worked example

Given that:

$$\sin A = \frac{8}{17} \text{ and } 0^\circ < A < 90^\circ, \text{ and}$$

$$\cos B = -\frac{4}{5}, B \text{ is obtuse,}$$

find the value of $\cos(A + B)$

Your turn

Given that:

$$\sin A = -\frac{3}{5} \text{ and } 180^\circ < A < 270^\circ, \text{ and}$$

$$\cos B = -\frac{12}{13}, B \text{ is obtuse,}$$

find the value of $\cos(A - B)$

$$\frac{33}{65}$$

Worked example

Given that:

$$\sin A = \frac{8}{17} \text{ and } 0^\circ < A < 90^\circ, \text{ and}$$

$$\cos B = -\frac{4}{5}, B \text{ is obtuse,}$$

find the value of $\tan(A - B)$

Your turn

Given that:

$$\sin A = -\frac{3}{5} \text{ and } 180^\circ < A < 270^\circ, \text{ and}$$

$$\cos B = -\frac{12}{13}, B \text{ is obtuse,}$$

find the value of $\tan(A + B)$

$$\frac{16}{63}$$

Worked example

Given that:

$$\sin A = \frac{8}{17} \text{ and } 0^\circ < A < 90^\circ, \text{ and}$$

$$\cos B = -\frac{4}{5}, B \text{ is obtuse,}$$

find the value of $\sec(A - B)$

Your turn

Given that:

$$\sin A = -\frac{3}{5} \text{ and } 180^\circ < A < 270^\circ, \text{ and}$$

$$\cos B = -\frac{12}{13}, B \text{ is obtuse,}$$

find the value of $\operatorname{cosec}(A + B)$

$$\frac{65}{16}$$

Worked example

Given that

$$2 \cos(x - 40)^\circ = \sin(x - 50)^\circ$$

show that $\tan x = 3 \tan 50^\circ$

Your turn

Given that

$$2 \cos(x + 50)^\circ = \sin(x + 40)^\circ$$

show that $\tan x = \frac{1}{3} \tan 40^\circ$

Shown