

6.3) Projection at any angle

Worked example

A particle P is projected from a point O on a horizontal plane with speed 56 ms^{-1} and with angle of elevation 45° . After projection, the particle moves freely under gravity until it strikes the plane at a point A . Find:

- (a) the greatest height above the plane reached by P
- (b) the time of flight of P
- (c) the distance OA

Your turn

A particle P is projected from a point O on a horizontal plane with speed 28 ms^{-1} and with angle of elevation 30° . After projection, the particle moves freely under gravity until it strikes the plane at a point A . Find:

- (a) the greatest height above the plane reached by P
- (b) the time of flight of P
- (c) the distance OA

a) 10 m

b) 2.9 s (2 sf)

c) 69 m (2 sf)

Worked example

A particle is projected from a point O with speed $V \text{ ms}^{-1}$ and at an angle of elevation of θ , where $\tan \theta = \frac{4}{3}$.

The point O is 42.5m above a horizontal plane. The particle strikes the plane at a point A , 5 s after it is projected.

- (a) Find V
- (b) Find the distance between O and A .

Your turn

A particle is projected from a point O with speed $V \text{ ms}^{-1}$ and at an angle of elevation of θ , where $\tan \theta = \frac{4}{3}$.

The point O is 42.5m above a horizontal plane. The particle strikes the plane at a point A , 5 s after it is projected.

- (a) Find V
- (b) Find the distance between O and A .

a) $V = 20$

b) 74 m (2 sf)

Worked example

A particle is projected from a point O with speed 70 ms^{-1} and at an angle of elevation of 45° .

The particle moves freely under gravity.

Find the length of time for which the particle is 30 m or more above O .

Your turn

A particle is projected from a point O with speed 35 ms^{-1} and at an angle of elevation of 30° .

The particle moves freely under gravity.

Find the length of time for which the particle is 15 m or more above O .

0.71 s (2 sf)

Worked example

A ball is struck by a racket at a point which is 2 m above horizontal ground. Immediately after the ball is struck, the ball has velocity $(10\mathbf{i} + 16\mathbf{j})\text{ms}^{-1}$ where \mathbf{i} and \mathbf{j} are unit vectors horizontally and vertically respectively.

After being struck, the ball travels freely under gravity until it strikes the ground.

Find:

- The greatest height above the ground reached by the ball
- The speed of the ball as it reaches the ground
- The angle the velocity of the ball makes with the ground as the ball reaches B

Your turn

A ball is struck by a racket at a point which is 4 m above horizontal ground. Immediately after the ball is struck, the ball has velocity $(5\mathbf{i} + 8\mathbf{j})\text{ms}^{-1}$ where \mathbf{i} and \mathbf{j} are unit vectors horizontally and vertically respectively.

After being struck, the ball travels freely under gravity until it strikes the ground.

Find:

- The greatest height above the ground reached by the ball
- The speed of the ball as it reaches the ground
- The angle the velocity of the ball makes with the ground as the ball reaches B

a) 5.3 m (2 sf)

b) 11 ms^{-1} (2 sf)

c) 64° (2 sf)

Worked example

A small stone is projected from a point at the top of a cliff, which is 8.4 m above the sea. The stone rises to a maximum height of 40 m above the top of the cliff before hitting the sea at a point which is 30 m from the foot of the cliff. The stone is modelled as a particle moving freely under gravity.

Find the speed of projection.

Your turn

A small stone is projected from a point at the top of a cliff, which is 52.5 m above the sea. The stone rises to a maximum height of 10 m above the top of the cliff before hitting the sea at a point which is 50 m from the foot of the cliff. The stone is modelled as a particle moving freely under gravity.

Find the speed of projection.

$$17\text{ ms}^{-1} \text{ (2 sf)}$$

Worked example

A particle is projected from a point on level ground with speed $U \text{ ms}^{-1}$ and an angle of elevation of α .
The maximum height reached by the particle is 15.3061 m (4 dp) above the ground and the particle hits the ground 35.3480 m (4 dp) from its point of projection.
Find the value of α and U

Your turn

A particle is projected from a point on level ground with speed $U \text{ ms}^{-1}$ and an angle of elevation of α .
The maximum height reached by the particle is 20.4082 m (4 dp) above the ground and the particle hits the ground 141.3919 m (4 dp) from its point of projection.
Find the value of α and U

$$\alpha = 30^\circ, U = 40$$