

## 5.2) Arc length

## Worked example

Find the length of the arc of a circle of radius 5.2 cm, given that the arc subtends an angle of 0.4 radians at the centre of the circle.

Find the length of the arc of a circle of radius 10.4 cm, given that the arc subtends an angle of 0.2 radians at the centre of the circle.

## Your turn

Find the length of the arc of a circle of radius 5.2 cm, given that the arc subtends an angle of 0.8 radians at the centre of the circle.

*4.16 cm*

## Worked example

An arc  $AB$  of a circle with radius 0.35 cm and centre  $O$  has a length of 2.45 cm. Find the angle  $\angle AOB$  subtended by the arc at the centre of the circle

An arc  $AB$  of a circle with radius 0.7 cm and centre  $O$  has a length of 4.9 cm. Find the angle  $\angle AOB$  subtended by the arc at the centre of the circle

## Your turn

An arc  $AB$  of a circle with radius 7 cm and centre  $O$  has a length of 2.45 cm. Find the angle  $\angle AOB$  subtended by the arc at the centre of the circle

*0.35 rad*

## Worked example

The border of a garden pond consists of a straight edge  $AB$  of length 4.8 m, and a curved part  $C$ , also connecting  $A$  and  $B$ . The curve part is an arc of a circle, centre  $O$ , radius 4 m.

Find the length of  $C$ .

## Your turn

The border of a garden pond consists of a straight edge  $AB$  of length 2.4 m, and a curved part  $C$ , also connecting  $A$  and  $B$ . The curve part is an arc of a circle, centre  $O$ , radius 2 m.

Find the length of  $C$ .

9.99 m

## Worked example

A triangle  $ABC$  is such that  $AB = 4 \text{ cm}$ ,  $AC = 5.5 \text{ cm}$  and  $\angle BAC = 0.35$  radians.

The arc  $BD$ , where  $D$  lies on  $AC$ , is an arc of a circle with centre  $A$  and radius  $4 \text{ cm}$ .

A region  $R$ , is bounded by the straight lines  $BC$  and  $CD$  and the arc  $BD$ .

Find the perimeter of  $R$

## Your turn

A triangle  $ABC$  is such that  $AB = 8 \text{ cm}$ ,  $AC = 11 \text{ cm}$  and  $\angle BAC = 0.7$  radians.

The arc  $BD$ , where  $D$  lies on  $AC$ , is an arc of a circle with centre  $A$  and radius  $8 \text{ cm}$ .

A region  $R$ , is bounded by the straight lines  $BC$  and  $CD$  and the arc  $BD$ .

Find the perimeter of  $R$

**15.7 cm (3 sf)**

## Worked example

A sector of a circle of radius 30 cm contains an angle of  $\theta$  radians. Given that the perimeter of the sector is 84 cm, find the value of  $\theta$

## Your turn

A sector of a circle of radius 15 cm contains an angle of  $\theta$  radians. Given that the perimeter of the sector is 42 cm, find the value of  $\theta$

$$\theta = 0.8 \text{ rad}$$

## Worked example

The perimeter of a sector OAB is four times the length of the arc AB. Find the size of angle AOB

## Your turn

The perimeter of a sector OAB is four times the length of the arc AB. Find the size of angle AOB

$$\theta = 2 \text{ rad}$$