

# Power

**Power** is the **rate of doing work** or **energy input per unit of time**

Using the second definition:

$$Power = \frac{energy}{time} = \frac{Force \times distance}{time} = Force \times velocity = \mathbf{Fv}$$

**Units:** Power is measured in Watts (W).  
A Watt is equivalent to a  $J s^{-1}$  or  $kg m^2 s^{-3}$ .

A van of mass 1250kg is travelling along a horizontal road. The van's engine is working at 24kW. The constant resistance to motion has a magnitude of 600N. Calculate :

- the acceleration of the van when it is travelling at  $6ms^{-1}$
- the maximum speed of the van.

A car of mass  $1100\text{kg}$  is travelling at a constant speed of  $15\text{ms}^{-1}$  along a straight road which is inclined at  $7^\circ$  to the horizontal. The engine is working at a rate of  $24\text{kW}$ .

a) Calculate the magnitude of the non-gravitational resistance to motion.

The rate of working of the engine is now increased to  $28\text{kW}$ .

Assuming the resistances to motion are unchanged,

b) Calculate the initial acceleration of the car.

A car of mass  $2600\text{kg}$  is travelling in a straight line. At the instant when the speed of the car is  $v\text{ ms}^{-1}$ , the total resistances to motion are modelled as a variable force of magnitude  $(800 + 5v^2)\text{N}$ . The car has a cruise control feature which adjusts the power generated by the engine to maintain a constant speed of  $18\text{ ms}^{-1}$ .

Find the power generated by the engine when:

- a) The car is travelling on a horizontal road
- b) The car is travelling up a road that is inclined at an angle  $4^\circ$  to the horizontal.

The rate of working of the engine is now increased to  $28\text{kW}$ .

Assuming the resistances to motion are unchanged,

- b) Calculate the initial acceleration of the car.

Ex 2D Q10-19

Side Note: Maximum speed is when acceleration is 0 - i.e. in equilibrium

A girl and her bicycle have a combined mass of 64 kg. She cycles up a straight stretch of road which is inclined at an angle  $\alpha$  to the horizontal, where  $\sin \alpha = \frac{1}{14}$ . She cycles at a constant speed of  $5 \text{ m s}^{-1}$ . When she is cycling at this speed, the resistance to motion from non-gravitational forces has magnitude 20 N.

(a) Find the rate at which the cyclist is working.

(4)

8. [In this question use  $g = 10 \text{ m s}^{-2}$ ]

Question	Mark	Answer
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A jogger of mass 60 kg runs along a straight horizontal road at a constant speed of  $4 \text{ m s}^{-1}$ . The total resistance to the motion of the jogger is modelled as a constant force of magnitude 30 N.

(a) Find the rate at which the jogger is working.

(3)

The jogger now comes to a hill which is inclined to the horizontal at an angle  $\alpha$ , where

$\sin \alpha = \frac{1}{15}$ . Because of the hill, the jogger reduces her speed to  $3 \text{ m s}^{-1}$  and maintains this

constant speed as she runs up the hill. The total resistance to the motion of the jogger from non-gravitational forces continues to be modelled as a constant force of magnitude 30 N.

(b) Find the rate at which she has to work in order to run up the hill at  $3 \text{ m s}^{-1}$ .

(5)