2.2) Completing the square

Worked example	Your turn
Complete the square for: $x^2 + 4x$	Complete the square for: $x^2 - 10x + 3$ $(x - 5)^2 - 22$
$x^2 - 6x$	
$x^2 + 8x - 7$	

Worked example	Your turn
Complete the square for: $x^2 + 6x + 5$	Complete the square for: $x^{2} + 10x + 1$ $(x + 5)^{2} - 24$
$x^2 + 8x + 3$	

Worked example	Your turn
Complete the square for: $x^2 - 6x + 5$	Complete the square for: $x^2 - 10x + 1$ $(x - 5)^2 - 24$
$x^2 - 8x - 3$	

Your turn
Complete the square for: $x^2 + 5x + 1$
$\left(x+\frac{5}{2}\right)^2 - \frac{21}{4}$

Worked example	Your turn
Complete the square for: $x^2 - 5x - 3$	Complete the square for: $x^2 - 3x - 2$ $\left(x - \frac{3}{2}\right)^2 - \frac{17}{4}$
$x^2 - x + 2$	

Worked example	Your turn
Complete the square for: $2x^2 + 12x + 1$	Complete the square for: $5x^2 + 40x + 3$ $5(x + 4)^2 - 77$
$3x^2 + 12x + 2$	

Worked example	Your turn
Complete the square for: $2x^2 + 5x + 1$	Complete the square for: $5x^2 + 9x + 3$
	$5\left(x+\frac{9}{10}\right)^2 - \frac{21}{20}$
$3x^2 + 7x + 2$	

Worked example	Your turn
Complete the square for: $2x^2 - 5x + 3$	Complete the square for: $3x^2 - 7x + 2$
	$3\left(x-\frac{7}{6}\right)^2 - \frac{25}{12}$
$5x^2 - 3x + 1$	

Worked example	Your turn
Express in the form $a(x + b)^2 + c$: $2x^2 - 5x + 3$	Express in the form $a(x + b)^2 + c$: $3x^2 - 7x + 2$
	$3\left(x-\frac{7}{6}\right)^2 - \frac{25}{12}$

Worked example	Your turn
Complete the square for: $3 + 5x - x^2$	Complete the square for: $5 - 7x - x^2$
	$-\left(x+\frac{7}{2}\right)^2+\frac{69}{4}$
$2 - 3x - x^2$	

Worked example	Your turn
Complete the square for: $3 + 5x - 2x^2$	Complete the square for: $5 - 7x - 3x^2$
	$-3\left(x+\frac{7}{6}\right)^2 + \frac{109}{12}$
$2 - 3x - 5x^2$	

Worked example	Your turn
Solve by completing the square: $x^2 + 8x + 3 = 0$	Solve by completing the square: $x^2 + 6x + 4 = 0$
	$x = -3 + \sqrt{5}, x = -3 - \sqrt{5}$
-10-10	
$x^{-} + 10x - 4 = 0$	

Worked example	Your turn
Solve by completing the square: $2x^2 - 8x + 3 = 0$	Solve by completing the square: $5x^{2} - 6x - 2 = 0$ $x = \frac{3 + \sqrt{19}}{5}, x = \frac{3 - \sqrt{19}}{5}$
$3x^2 - 10x - 4 = 0$	

Worked example	Your turn
Solve using three methods: $x^2 + 6x + 8 = 0$	Solve using three methods: $x^{2} + 6x + 5 = 0$ x = -5, x = -1
$x^2 + 6x + 8 = 0$	
$x^2 + 6x + 8 = 0$	

Worked example	Your turn
By completing the square, explain why the curve $y = 2x^2 - 8x + 9$ does not intersect the <i>x</i> -axis	By completing the square, explain why the curve $y = 2x^2 - 20x +$ 51 does not intersect the <i>x</i> -axis
	$y = 2(x - 5)^2 + 1$ Turning point at (5, 1)

Worked example	Your turn
A sequence has the n th term	A sequence has the n th term
$n^2 - 6n + 10.$	$n^2 - 10n + 27.$
By completing the square, show	By completing the square, show
that every term is positive.	that every term is positive.
	$n^2 - 10n + 27 = (n - 5)^2 + 2$

 $k^2 \ge 0$ $(n-5)^2 \ge 0$ $(n-5)^2 + 2 \ge 2$