

9.2) Equation of a plane in three dimensions

Worked example

A plane Π passes through the points

$$A(1, -2, 2), B(-3, -2, 1), C(5, 4, 3)$$

Find the equation of the plane Π in the form

$$r = \mathbf{a} + \lambda \mathbf{b} + \mu \mathbf{c}$$

Your turn

A plane Π passes through the points

$$A(2, 2 - 1), B(3, 2, -1), C(4, 3, 5)$$

Find the equation of the plane Π in the form

$$r = \mathbf{a} + \lambda \mathbf{b} + \mu \mathbf{c}$$

$$r = 2\mathbf{i} + 2\mathbf{j} - \mathbf{k} + \lambda \mathbf{i} + \mu(2\mathbf{i} + \mathbf{j} + 6\mathbf{k})$$

$$r = \begin{pmatrix} 2 \\ 2 \\ -1 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} + \mu \begin{pmatrix} 2 \\ 1 \\ 6 \end{pmatrix}$$

Worked example

Verify that the point P with position vector $\begin{pmatrix} 2 \\ -3 \\ 2 \end{pmatrix}$

lies in the plane with vector equation

$$r = \begin{pmatrix} 3 \\ 4 \\ -2 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} + \mu \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix}$$

Your turn

Verify that the point P with position vector $\begin{pmatrix} 2 \\ 2 \\ -1 \end{pmatrix}$

lies in the plane with vector equation

$$r = \begin{pmatrix} 3 \\ 4 \\ -2 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} + \mu \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix}$$

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