## 8A Introduction to Proof by Induction

1. Prove by mathematical induction that, for $n \in \mathbb{Z}^{+}$

$$
\sum_{r=1}^{n}(2 r-1)=n^{2}
$$

2. Prove, by mathematical induction, that for $n \in \mathbb{Z}^{+}$,

$$
\sum_{r=1}^{n}\left(r^{2}\right)=\frac{1}{6} n(n+1)(2 n+1)
$$

3. Prove, by mathematical induction, that for $n \in \mathbb{Z}^{+}$,

$$
\sum_{r=1}^{n}\left(r 2^{r}\right)=2\left[1+(n-1) 2^{n}\right]
$$

