

7.4) Successive transformations

Worked example

Represent as a single matrix the transformation representing a reflection in the line $y = x$ followed by a stretch parallel to the x -axis by a factor of 4.

Represent as a single matrix the transformation representing a rotation 90° anticlockwise about the point $(0,0)$ followed by a reflection in the line x -axis.
What single transformation is this?

Your turn

Represent as a single matrix the transformation representing a reflection in the line $y = -x$ followed by a stretch parallel to the y -axis by a factor of 3.

$$\begin{pmatrix} 0 & -3 \\ -1 & 0 \end{pmatrix}$$

Represent as a single matrix the transformation representing a rotation 270° anticlockwise about the point $(0,0)$ followed by a reflection in the line y -axis.
What single transformation is this?

$$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

Reflection in the line $y = -x$

Worked example

The matrix R is given by $R = \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$

- Find R^3
- Describe the geometric transformation represented by R^3
- Hence describe the geometric transformation represented by R
- Write down R^{900}

Your turn

The matrix R is given by $R = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$

- Find R^2
- Describe the geometric transformation represented by R^2
- Hence describe the geometric transformation represented by R
- Write down R^8

a) $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$

b) Rotation 90° anticlockwise about $(0, 0)$

c) Rotation 45° anticlockwise about $(0, 0)$

d) $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} = I$