Matrices and their Inverses

Determinants

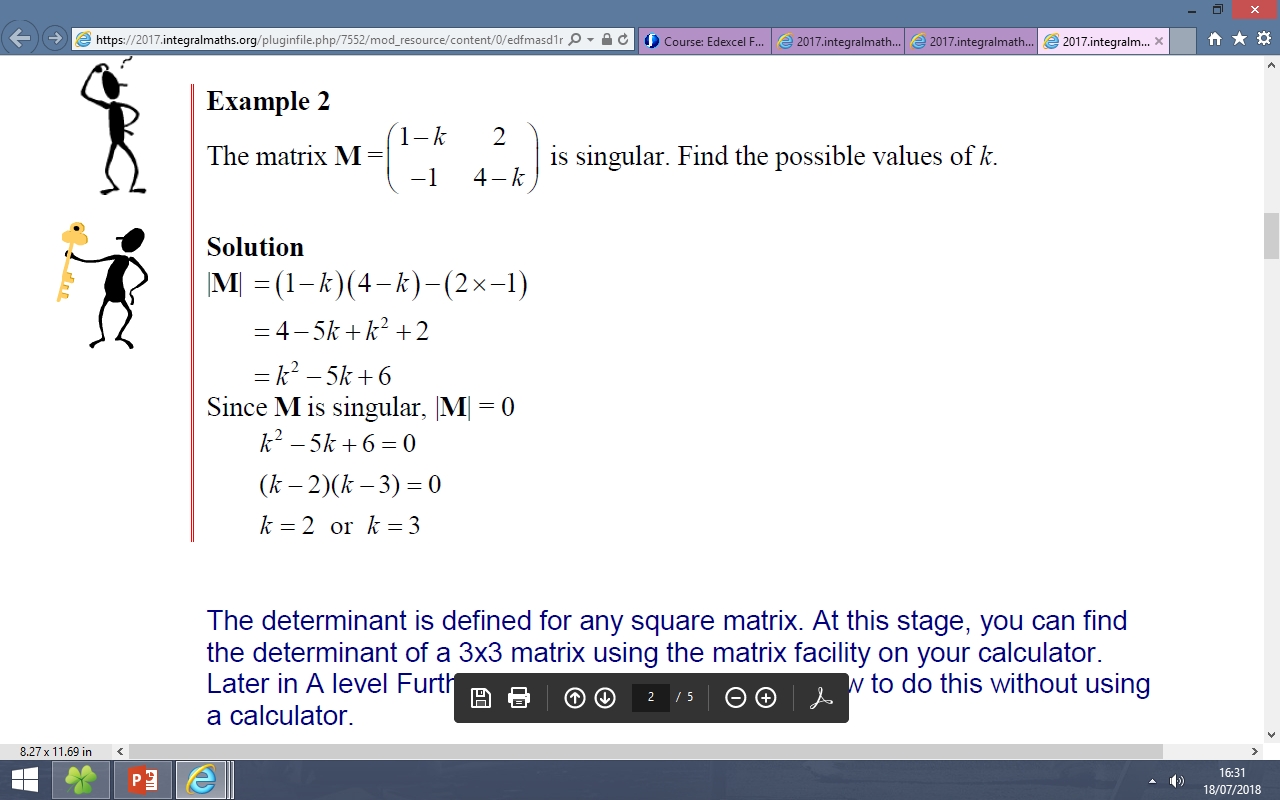
* The determinant of a matrix has many applications in matrices. Fundamentally, the determinant is required to find the inverse of a matrix.
* The determinant of a matrix is

* If , then is a **singular matrix** and it does not have an inverse.
* If , then is a **non-singular matrix** and it has an inverse.

Quickfire Questions:

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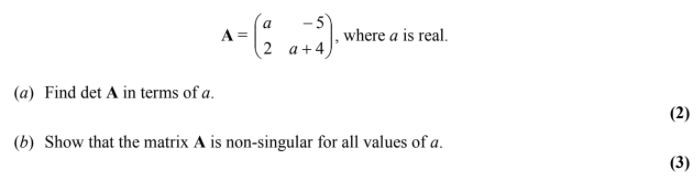
Example



Example

Given that is singular, find the value of .

Test Your Understanding



Determinants of 3x3 Matrices

To find the determinant and inverse of a 3 x 3 matrix, it is first necessary to define some new terms.

* **The minor of an element**

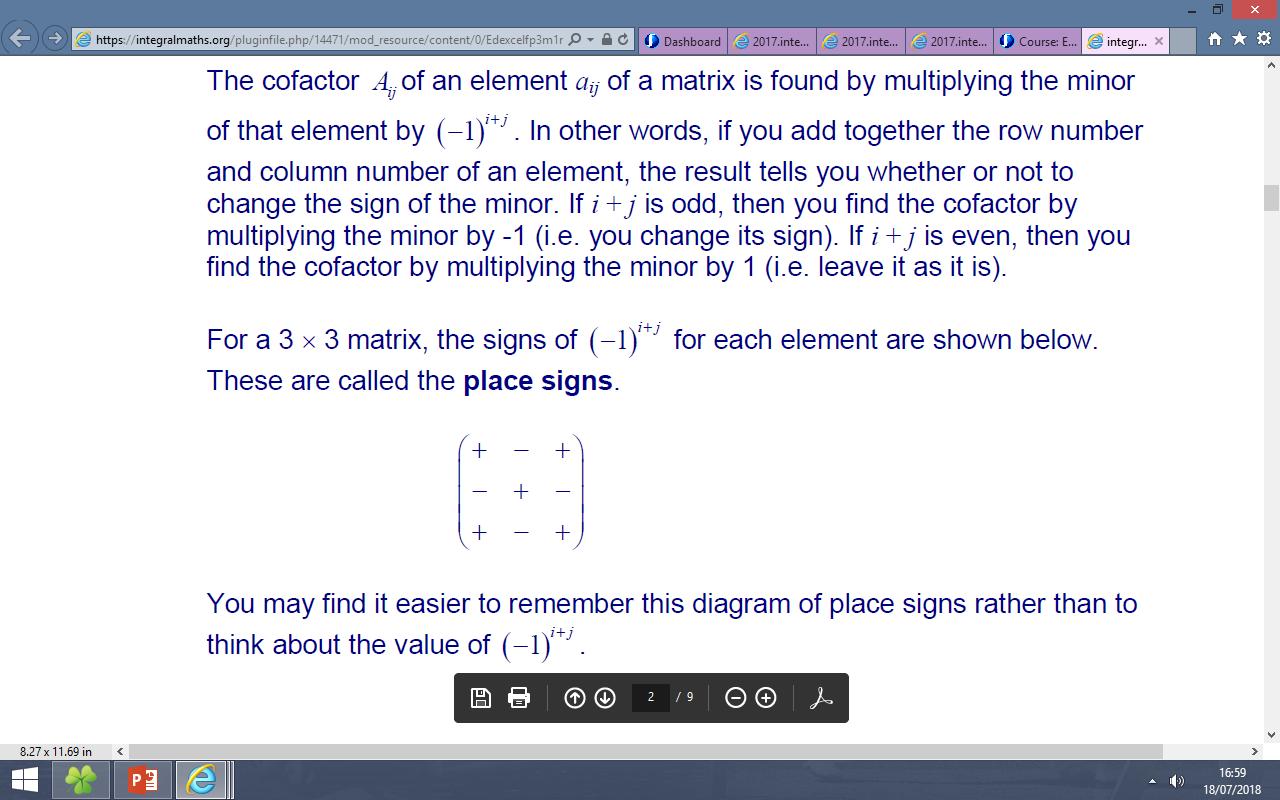
The minor of a particular element of a matrix is found by eliminating the row and column of that element and finding the determinant of the remaining matrix.

For a 3 x 3 matrix, the remaining matrix will be a 2 x 2 matrix.

* **The cofactors of an element**

The cofactor of an element is its minor multiplied by a multiple of

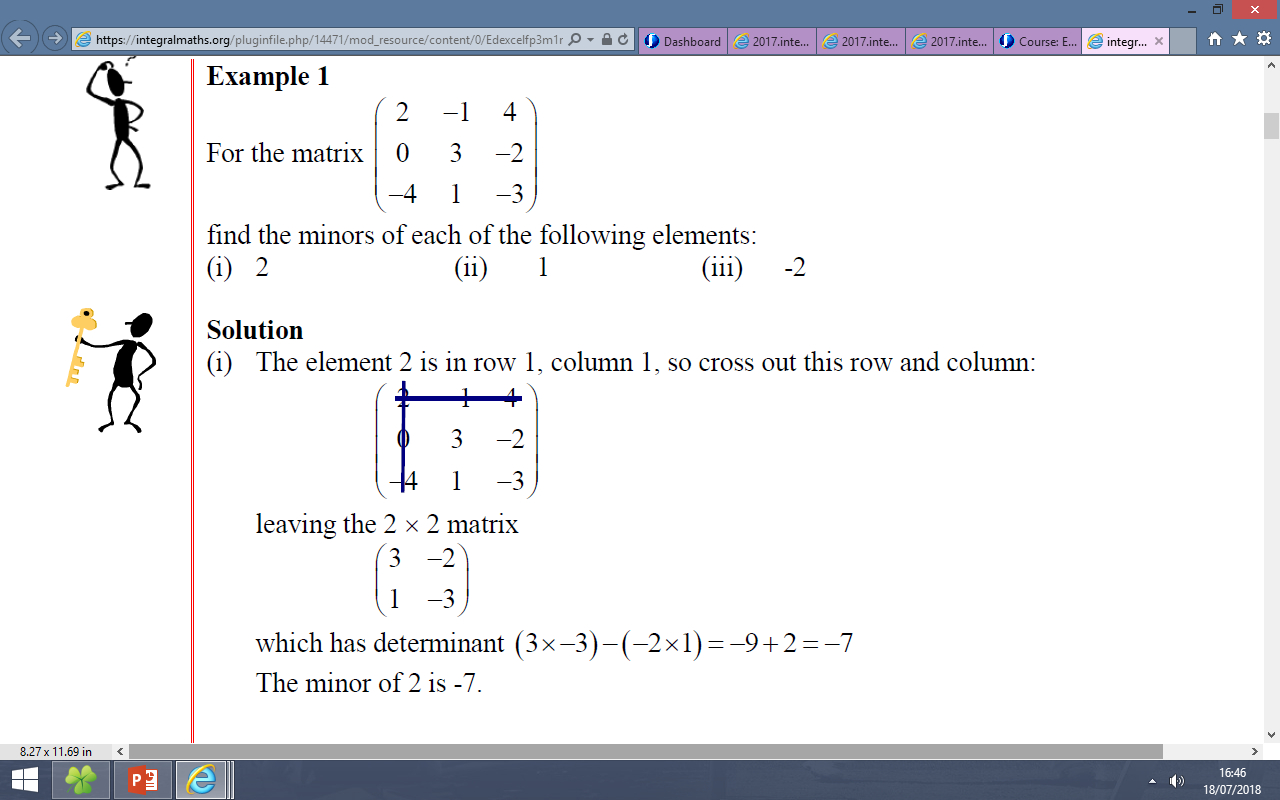
(-1) in the following pattern (called the place signs)

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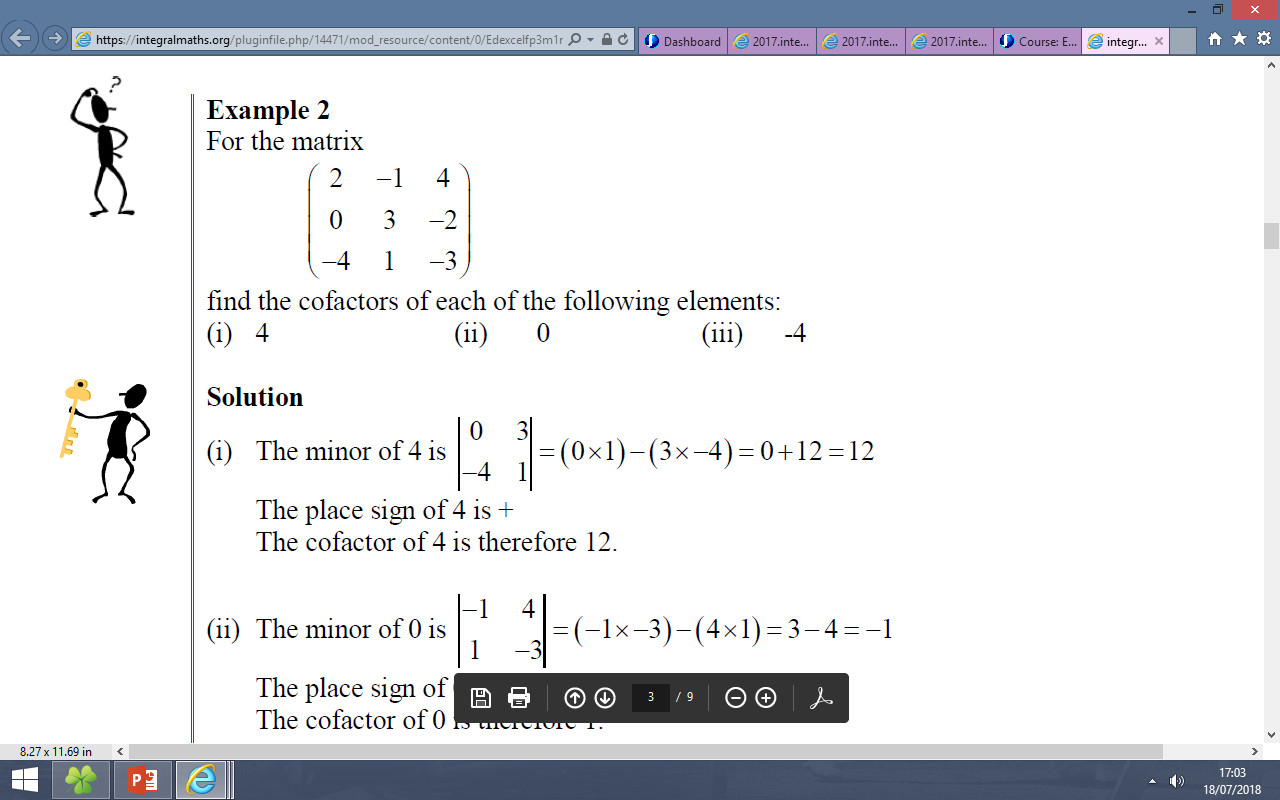
Example

Find the minors of the elements 0, -6 and 5 in the below matrix:

Test Your Understanding

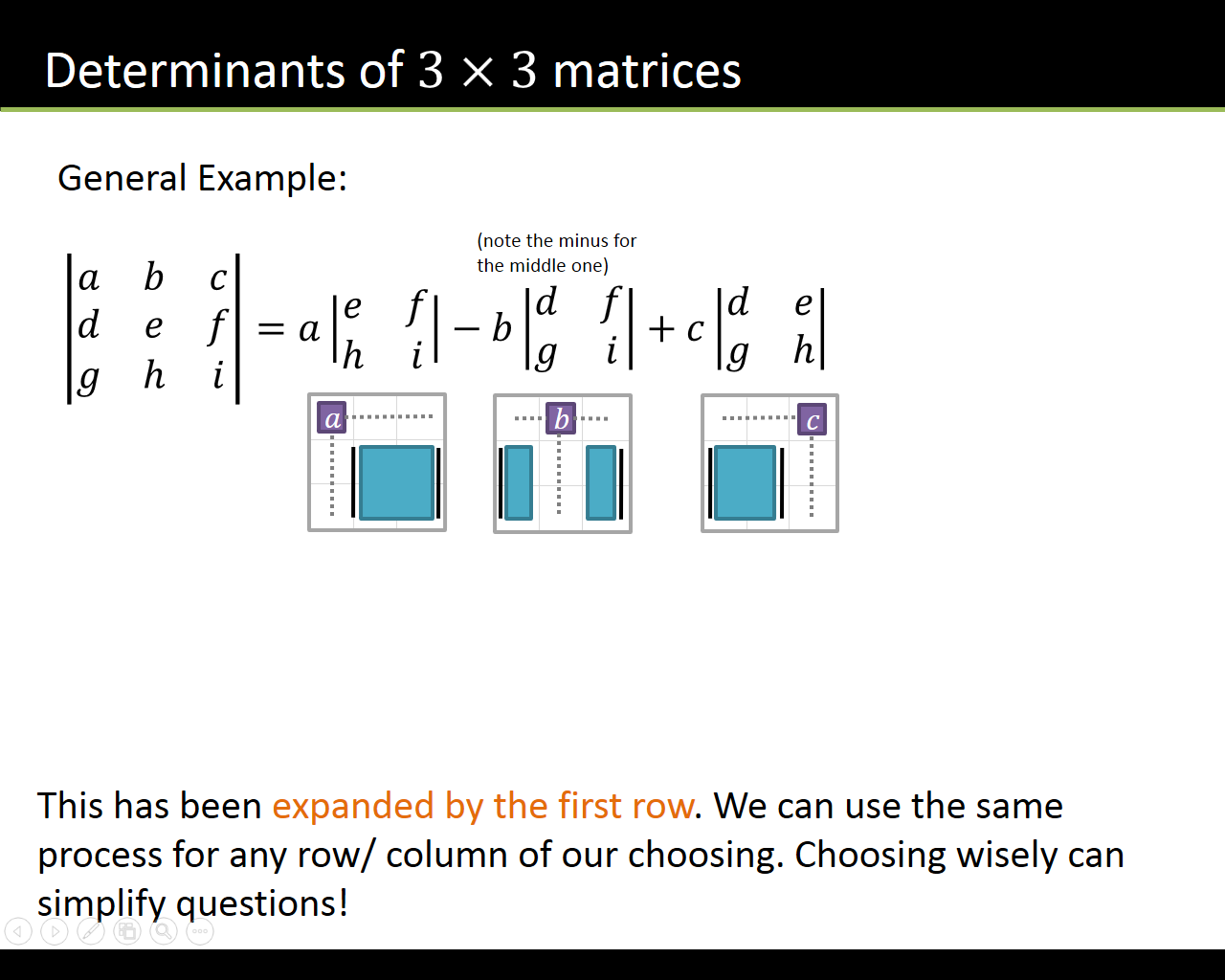


Example



Finding the determinant

The determinant of a 3 x 3 matrix can be found from the cofactors of any row or column of the matrix. Each element in that row or column is multiplied by its cofactor, and the results are added together.



Example

Test Your Understanding

1.

Determine .

2.

where is a constant.

Given that is singular, find the possible values of .

Alternative Method:

Ex 6C Pg 108