

## 5.2) Volumes of revolution around the $y$ -axis

## Worked example

A curve has equation  $y = \sqrt{x - 2}$ . A finite region is bounded by the curve, the  $y$ -axis and the lines  $y = 1$  and  $y = 4$ . The region is rotated through  $360^\circ$  about the  $y$ -axis. Find the volume of the solid generated.

## Your turn

A curve has equation  $y = \sqrt{x - 1}$ . A finite region is bounded by the curve, the  $y$ -axis and the lines  $y = 1$  and  $y = 3$ . The region is rotated through  $360^\circ$  about the  $y$ -axis. Find the volume of the solid generated.

$$\frac{1016\pi}{15}$$

## Worked example

A curve has equation  $y = \sqrt[3]{3x + 1}$ . A finite region is bounded by the curve, the  $y$ -axis and the lines  $y = 2$  and  $y = 5$ . The region is rotated through  $360^\circ$  about the  $y$ -axis. Find the volume of the solid generated.

## Your turn

A curve has equation  $y = \sqrt[3]{2x + 1}$ . A finite region is bounded by the curve, the  $y$ -axis and the lines  $y = 2$  and  $y = 4$ . The region is rotated through  $360^\circ$  about the  $y$ -axis. Find the volume of the solid generated.

$$\frac{7715\pi}{14}$$

## Worked example

A curve has equation  $x = y^2 - 4y + 8$ . A finite region is bounded by the curve, the  $y$ -axis and the lines  $y = 1$  and  $y = 5$ .

- a) Find the area of the region
- b) The region is rotated through  $360^\circ$  about the  $y$ -axis. Find the volume of the solid generated.

## Your turn

A curve has equation  $x = y^2 - 6y + 10$ . A finite region is bounded by the curve, the  $y$ -axis and the lines  $y = 1$  and  $y = 4$ .

- a) Find the area of the region
- b) The region is rotated through  $360^\circ$  about the  $y$ -axis. Find the volume of the solid generated.

a) 6

b)  $\frac{78}{5}\pi$

## Worked example

$$f(x) = x^2 - 6x + 9, x \geq 3$$

A finite region is bounded by the curve  $y = f(x)$ , the  $y$ -axis and the lines  $y = 1$  and  $y = 4$ . The region is rotated through  $2\pi$  radians about the  $y$ -axis. Find the exact volume of the solid generated.

## Your turn

$$f(x) = x^2 - 2x + 1, x \geq 1$$

A finite region is bounded by the curve  $y = f(x)$ , the  $y$ -axis and the lines  $y = 1$  and  $y = 9$ . The region is rotated through  $2\pi$  radians about the  $y$ -axis. Find the exact volume of the solid generated.

$$\frac{248}{3}\pi$$

## Worked example

A curve has equation  $y^2 = \frac{1}{3x+2}$

A finite region is bounded by the curve  $y = f(x)$ , the  $y$ -axis and the line  $y = 5$

The region is rotated through  $2\pi$  radians about the  $y$ -axis. Find the volume of the solid generated.

## Your turn

A curve has equation  $y^2 = \frac{1}{2x+1}$

A finite region is bounded by the curve  $y = f(x)$ , the  $y$ -axis and the line  $y = 4$

The region is rotated through  $2\pi$  radians about the  $y$ -axis. Find the volume of the solid generated.

$$\frac{117}{256}\pi$$