

## Integrating with inverse trigonometric functions

Use an appropriate substitution to show that  $\int \frac{1}{1+x^2} dx = \arctan x + C$

Think what value of  $x$  would make  $1 + x^2$  nicely simplify.

Dealing with  $1/(a^2 - x^2)$ ,  $1/\sqrt{a^2 - x^2}$ , ....

Use our previous results to fill in the table below:

$$\int \frac{1}{\sqrt{1-x^2}} dx = \qquad |x| < a$$
$$\int \frac{1}{1+x^2} dx =$$

Show that  $\int \frac{1}{\sqrt{a^2-x^2}} dx = \arcsin\left(\frac{x}{a}\right) + c$  where  $a$  is a positive constant and  $|x| < a$ .

We can extend these results to give some standard results which are given in the formulae book:

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \arcsin\left(\frac{x}{a}\right) + C, \quad |x| < a$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \arctan\left(\frac{x}{a}\right) + C$$

1. Find  $\int \frac{4}{5+x^2} dx$

2. Find  $\int \frac{1}{25+9x^2} dx$

3. Find  $\int_{-\frac{\sqrt{3}}{4}}^{\frac{\sqrt{3}}{4}} \frac{1}{\sqrt{3-4x^2}} dx$

4. Find  $\int \frac{x+4}{\sqrt{1-4x^2}} dx$