

Worked example

$$z_1 = 6\left(\cos \frac{5\pi}{12} + i \sin \frac{5\pi}{12}\right)$$

$$z_2 = 3\left(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4}\right)$$

Find:

i) $|z_1 z_2|$

ii) $\arg(z_1 z_2)$

iii) $z_1 z_2$ in the form $r(\cos \theta + i \sin \theta)$

iv) $z_1 z_2$ in the form $x + iy$

Your turn

$$z_1 = 8\left(\cos \frac{7\pi}{10} + i \sin \frac{7\pi}{10}\right)$$

$$z_2 = 4\left(\cos \frac{4\pi}{5} + i \sin \frac{4\pi}{5}\right)$$

Find:

i) $|z_1 z_2|$ 32

ii) $\arg(z_1 z_2)$ - $\frac{\pi}{2}$

iii) $z_1 z_2$ in the form $r(\cos \theta + i \sin \theta)$

$32 \left(\cos \left(-\frac{\pi}{2} \right) + i \sin \left(-\frac{\pi}{2} \right) \right)$

iv) $z_1 z_2$ in the form $x + iy$

-32i

Worked example

$$z_1 = 6\left(\cos \frac{5\pi}{12} + i \sin \frac{5\pi}{12}\right)$$

$$z_2 = 3\left(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4}\right)$$

Find:

i) $\left| \frac{z_1}{z_2} \right|$

ii) $\arg\left(\frac{z_1}{z_2}\right)$

iii) $\frac{z_1}{z_2}$ in the form $r(\cos \theta + i \sin \theta)$

iv) $\frac{z_1}{z_2}$ in the form $x + iy$

Your turn

$$z_1 = 8\left(\cos \frac{7\pi}{10} + i \sin \frac{7\pi}{10}\right)$$

$$z_2 = 4\left(\cos \frac{4\pi}{5} + i \sin \frac{4\pi}{5}\right)$$

Find:

i) $\left| \frac{z_1}{z_2} \right|$

2

ii) $\arg\left(\frac{z_1}{z_2}\right)$ $-\frac{\pi}{10}$

iii) $\frac{z_1}{z_2}$ in the form $r(\cos \theta + i \sin \theta)$

$2\left(\cos\left(-\frac{\pi}{10}\right) + i \sin\left(-\frac{\pi}{10}\right)\right)$

iv) $\frac{z_1}{z_2}$ in the form $x + iy$

1.90 – 0.618i

Worked example

$$z_1 = 6\left(\cos \frac{5\pi}{12} - i \sin \frac{5\pi}{12}\right)$$

$$z_2 = 3\left(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4}\right)$$

Find:

i) $|z_1 z_2|$

ii) $\arg(z_1 z_2)$

iii) $z_1 z_2$ in the form $r(\cos \theta + i \sin \theta)$

iv) $z_1 z_2$ in the form $x + iy$

Your turn

$$z_1 = 8\left(\cos \frac{7\pi}{10} + i \sin \frac{7\pi}{10}\right)$$

$$z_2 = 4\left(\cos \frac{4\pi}{5} - i \sin \frac{4\pi}{5}\right)$$

Find:

i) $|z_1 z_2|$ 32

ii) $\arg(z_1 z_2)$ - $\frac{\pi}{10}$

iii) $z_1 z_2$ in the form $r(\cos \theta + i \sin \theta)$

32 \left(\cos \left(-\frac{\pi}{10} \right) + i \sin \left(-\frac{\pi}{10} \right) \right)

iv) $z_1 z_2$ in the form $x + iy$

30.4 - 9.89i