2D Composite Maclaurin Series

Formula Book Formulae:

Maclaurin's and Taylor's Series

$$f(x) = f(0) + x\,f'(0) + \frac{x^2}{2!}f''(0) + \ldots + \frac{x^r}{r!}f^{(r)}(0) + \ldots$$

$$e^x = \exp(x) = 1 + x + \frac{x^2}{2!} + \ldots + \frac{x^r}{r!} + \ldots \qquad \text{for all } x$$

$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \ldots + (-1)^{r+1}\frac{x^r}{r} + \ldots \qquad (-1 < x \leqslant 1)$$

$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \ldots + (-1)^r \frac{x^{2r+1}}{(2r+1)!} + \ldots \qquad \text{for all } x$$

$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \ldots + (-1)^r \frac{x^{2r}}{(2r)!} + \ldots \qquad \text{for all } x$$

$$\arctan x = x - \frac{x^3}{3} + \frac{x^5}{5} - \ldots + (-1)^r \frac{x^{2r+1}}{2r+1} + \ldots \qquad (-1 \leqslant x \leqslant 1)$$

1. Write down the first 4 non-zero terms in the series expansion of $\cos(2x^2)$

2. Find the first 4 non-zero terms in the series expansion of:

$$ln\left\{\frac{\sqrt{1+2x}}{1-3x}\right\}$$

3. Given that terms in x^n, $n > 4$ can be ignored, show, using the series expansions of e^x and $\sin x$, that:

$$e^{sinx} \approx 1 + x + \frac{x^2}{2} - \frac{x^4}{8}$$