

## 2.3) Modulus-argument form of complex numbers

## Worked example

Express  $z = -1 + i$  in the form  $r(\cos \theta + i \sin \theta)$  where  $-\pi < \theta \leq \pi$

## Your turn

Express  $z = -1 - i$  in the form  $r(\cos \theta + i \sin \theta)$  where  $-\pi < \theta \leq \pi$

$$r = \sqrt{2} \left( \cos \left( -\frac{3\pi}{4} \right) + i \sin \left( -\frac{3\pi}{4} \right) \right)$$

## Worked example

Express  $z = -\sqrt{3} + i$  in the form  $r(\cos \theta + i \sin \theta)$  where  $-\pi < \theta \leq \pi$

## Your turn

Express  $z = -1 - \sqrt{3}i$  in the form  $r(\cos \theta + i \sin \theta)$  where  $-\pi < \theta \leq \pi$

$$r = 2 \left( \cos \left( -\frac{2\pi}{3} \right) + i \sin \left( -\frac{2\pi}{3} \right) \right)$$

## Worked example

The complex number  $z$  is such that  $|z| = 3$  and  $\arg z = \frac{\pi}{4}$ . Find  $z$  in the form  $a + bi$ , where  $a$  and  $b$  are exact real numbers to be found.

The complex number  $z$  is such that  $|z| = 4$  and  $\arg z = -\frac{3\pi}{4}$ . Find  $z$  in the form  $a + bi$ , where  $a$  and  $b$  are exact real numbers to be found.

## Your turn

The complex number  $z$  is such that  $|z| = 5$  and  $\arg z = \frac{3\pi}{4}$ . Find  $z$  in the form  $a + bi$ , where  $a$  and  $b$  are exact real numbers to be found.

$$a = -\frac{5\sqrt{2}}{2}, b = \frac{5\sqrt{2}}{2}$$