## 7E 3D Transformations



1. A transformation $U$, in three dimensions, represents a reflection in the plane $z=0$.
a) Write down the $3 \times 3$ matrix that represents this transformation.
b) Find the image of the point $(-1,2,3)$ under this transformation

Reflection in the $y z$ plane $(x=0)$

Reflection in the $x z$ plane $(y=0)$

Reflection in the $x y$ plane $(z=0)$
2. A transformation $U$, in three dimensions, represents a $90^{\circ}$ anticlockwise rotation around the $x$-axis
a) Write down the $3 \times 3$ matrix that represents this transformation.
b) Find the image of the point $(-1,2,3)$ under this transformation

Rotation anticlockwise $\theta$ around the x -axis

Rotation anticlockwise $\theta$ around the $y$-axis

Rotation anticlockwise $\theta$ around the $z$-axis
3. The matrix $\boldsymbol{M}=\left[\begin{array}{ccc}\frac{\sqrt{3}}{2} & 0 & \frac{1}{2} \\ 0 & 1 & 0 \\ -\frac{1}{2} & 0 & \frac{\sqrt{3}}{2}\end{array}\right]$.
a) Describe the transformation represented by $\boldsymbol{M}$.
b) Find the image of the point with coordinates $(-1,-2,1)$ under the transformation represented by $\boldsymbol{M}$.

