## Combined Transformations

$\square$

Examples

1. Represent as a single matrix the transformation representing a reflection in the line $y=x$ followed by a stretch on the $x$ axis by a factor of 4 .
2. Represent as a single matrix the transformation representing a rotation $90^{\circ}$ anticlockwise about the point $(0,0)$ followed by a reflection in the line $y=x$.

## Test Your Understanding

The transformation $U$, represented by the $2 \times 2$ matrix $\mathbf{P}$, is a rotation through $90^{\circ}$ anticlockwise about the origin.
(a) Write down the matrix $\mathbf{P}$.

The transformation $V$, represented by the $2 \times 2$ matrix $\mathbf{Q}$, is a reflection in the line $y=-x$.
(b) Write down the matrix $\mathbf{Q}$.
(1)

Given that $U$ followed by $V$ is transformation $T$, which is represented by the matrix $\mathbf{R}$,
(c) express $\mathbf{R}$ in terms of $\mathbf{P}$ and $\mathbf{Q}$,
(1)
(d) find the matrix $\mathbf{R}$,
(e) give a full geometrical description of $T$ as a single transformation.

