

## Problem solving with sin/cos rule

### Example

The diagram shows the locations of four mobile phone masts in a field,  $BC = 75 \text{ m}$ .  $CD = 80 \text{ m}$ , angle  $BCD = 55^\circ$  and angle  $ADC = 140^\circ$ .

In order that the masts do not interfere with each other, they must be at least 70m apart.

Given that  $A$  is the minimum distance from  $D$ , find:

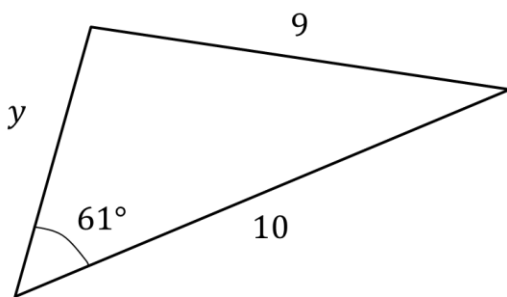
- a) The distance  $A$  is from  $B$
- b) The angle  $BAD$
- c) The area enclosed by the four masts.

Using the sine rule twice:

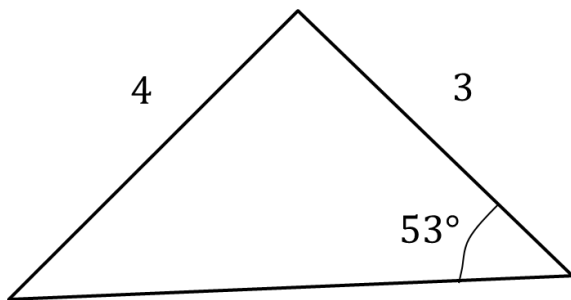
Test  
your

understanding

1.



2.



## Extension

1. [AEA 2009 Q5a] The sides of the triangle  $ABC$  have lengths  $BC = a$ ,  $AC = b$  and  $AB = c$ , where  $a < b < c$ . The sizes of the angles  $A$ ,  $B$  and  $C$  form an arithmetic sequence.

(i) Show that the area of triangle  $ABC$  is  $ac \frac{\sqrt{3}}{4}$ .

Given that  $a = 2$  and  $\sin A = \frac{\sqrt{15}}{5}$ , find

(ii) the value of  $b$ ,

(iii) the value of  $c$ .