

7C Double Angles Formulae

$$\sin 2A \equiv 2\sin A \cos A$$

Key points:

If you see sin and cos multiplied together and both have the same angle -> this can be reduced using sin double angle formulae to a single trig function

Examples:

a) $\sin x \cos x =$

b) $6 \cos x \sin x =$

c) $5 \sin 3x \cos 3x =$

$$\cos 2A \equiv \cos^2 A - \sin^2 A$$

Key points:

If you see $\sin^2 A$ or $\cos^2 A$ this can be reduced using the cos double angle formulae to a single trig function

Examples:

a) $\sin^2 x =$

b) $4\cos^2 x =$

c) $3\sin^2 4x =$

$$\tan 2A \equiv \frac{2\tan A}{1-\tan^2 A}$$

1. Use the double angle formulae to write the following expression as a single trigonometric ratio:

a) $\cos^2 50 - \sin^2 50$

b) $\frac{2\tan\frac{\pi}{6}}{1-\tan^2\frac{\pi}{6}}$

c) $\frac{4\sin 70}{\sec 70}$

2. Given that $x = 3\sin\theta$ and $y = 3 - 4\cos 2\theta$, eliminate θ and express y in terms of x .

3. Given that:

$$\cos x = \frac{3}{4}, \quad 180^\circ < x < 360^\circ$$

Find the exact value of:

a) $\sin 2x$

b) $\tan 2x$