

6A Reciprocal Trigonometric Functions

1. Will $\operatorname{cosec}(200)$ be positive or negative?

2. Find the value of:

a) $\sec(280)$

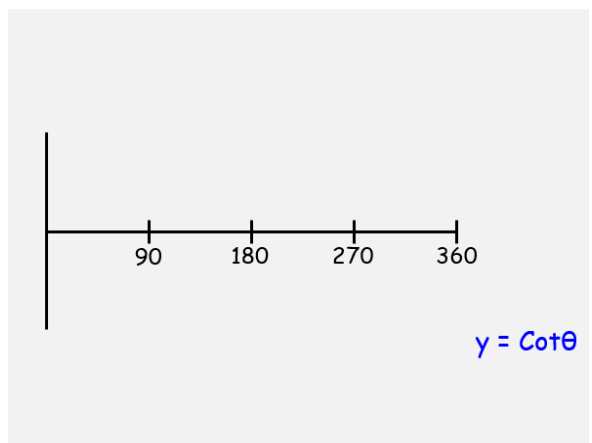
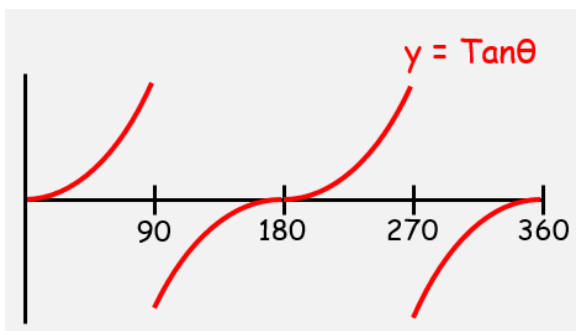
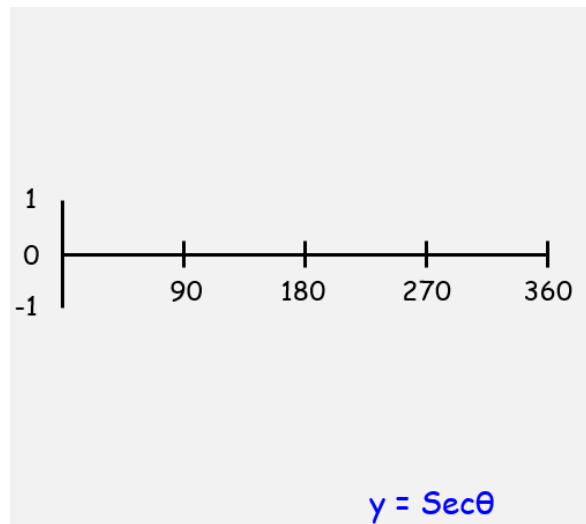
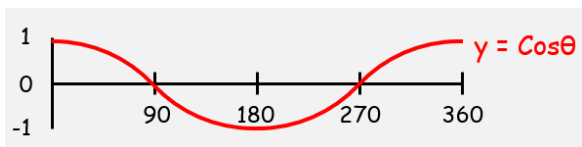
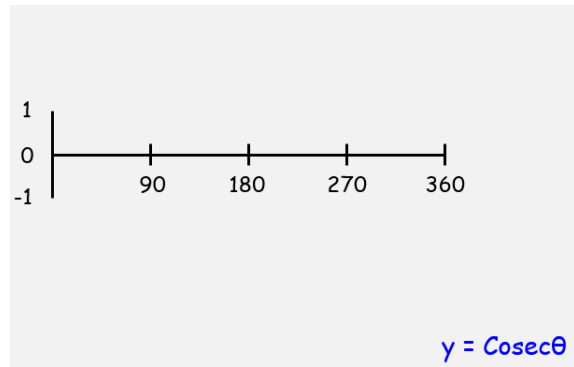
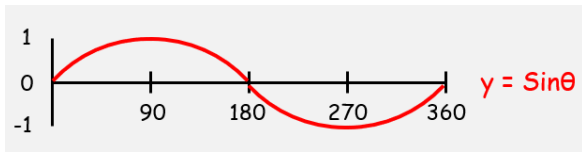
b) $\cot(115)$

3. Work out the exact value of:

a) $\sec(210)$

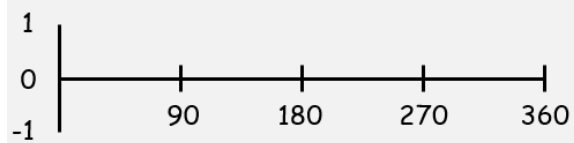
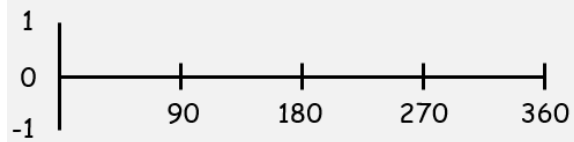
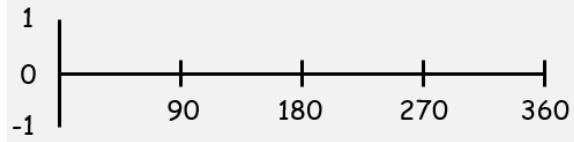
b) $\operatorname{cosec}\left(\frac{3\pi}{4}\right)$

6B Reciprocal Trigonometric Graphs



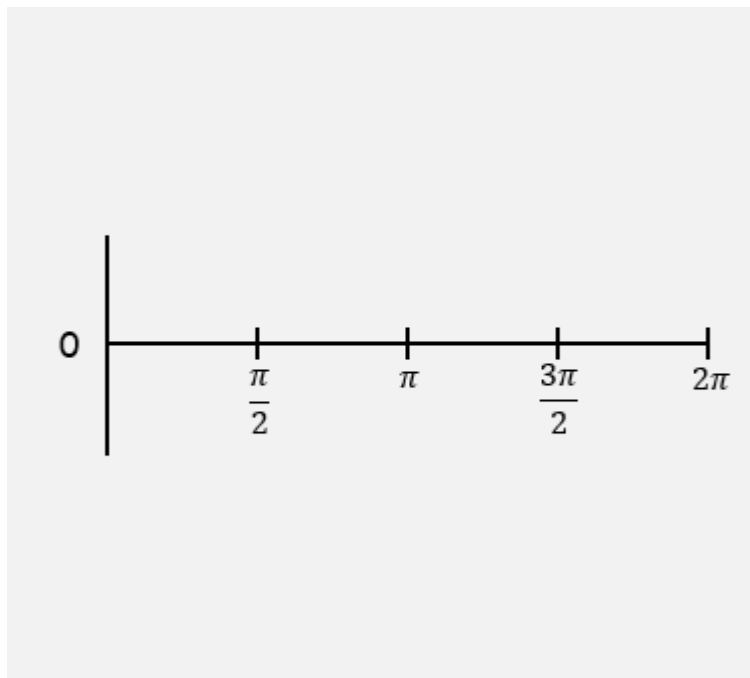
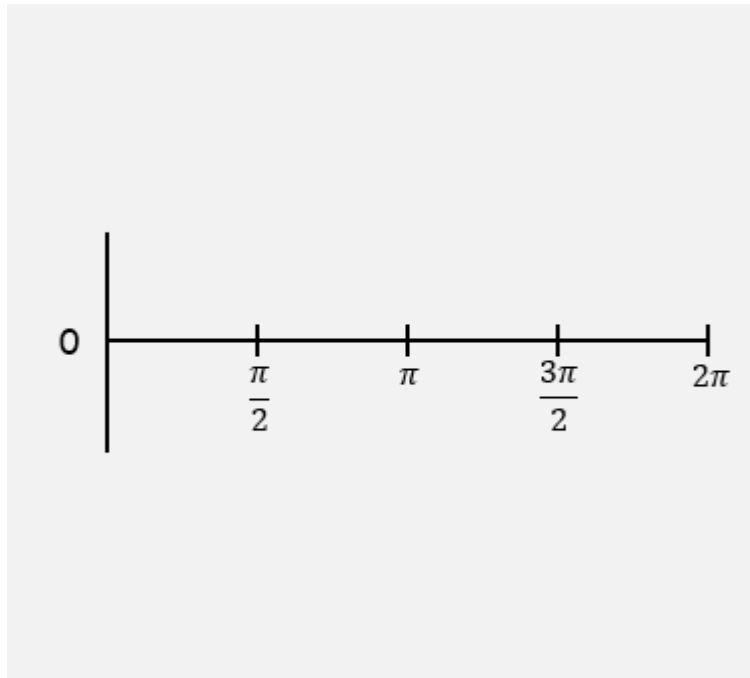
1. Sketch, in the interval $0 \leq \theta \leq 360$, the graph of:

$$y = 1 + \sec(2\theta)$$



2. Sketch the graph of:

a) $y = 4\operatorname{cosec}x$, $0 \leq x \leq 2\pi$



b) On the same axes, sketch the line $y = x$

c) State the number of solutions to the equation:

$$4\operatorname{cosec}x - x = 0 \quad 0 \leq x \leq 2\pi$$

6C Part 1 Simplifying Expressions

1. simplify

a) $\sin\theta \cot\theta \sec\theta$

b) $\sin\theta \cos\theta (\sec\theta + \operatorname{cosec}\theta)$

$$c) \frac{\cot\theta \operatorname{cosec}\theta}{\sec^2\theta + \operatorname{cosec}^2\theta} \equiv \cos^3\theta$$

6C Part 2 Solving Equations

2. Solve the equation

d) $\sec\theta = -2.5$ in the range $0 \leq \theta \leq 360$

e) $\cot 2\theta = 0.6$ in the range $0 \leq \theta \leq 360$

f) $3\operatorname{cosec}\theta = 2\sec\theta$ in the range $0 \leq \theta \leq 360$

6D Part 1 Exact Trig Values

3. Given that

$$\tan A = -\frac{5}{12}$$

and A is obtuse, find the exact value of

a) $\sec A$

b) $\operatorname{cosec} A$

4. Given that

$$\cot B = \frac{7}{24}$$

and B is reflex, find the exact value of

a) $\sec B$

b) $\operatorname{cosec} B$

6D Part 2 Reciprocal Trigonometric Identities

1. Prove that

$$\operatorname{cosec}^4\theta - \cot^4\theta \equiv \frac{1 + \cos^2\theta}{1 - \cos^2\theta}$$

2. Prove that

$$\sec^2\theta - \cos^2\theta \equiv \sin^2\theta(1 + \sec^2\theta)$$

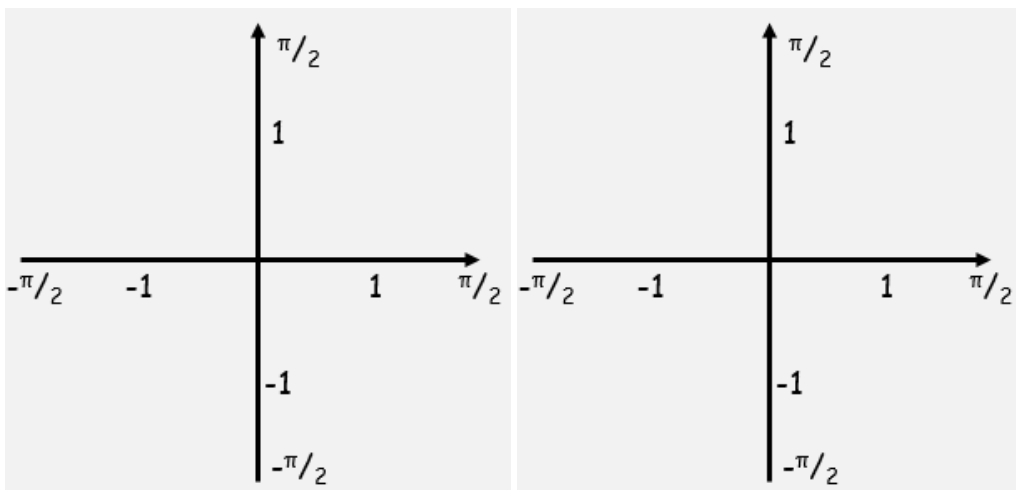
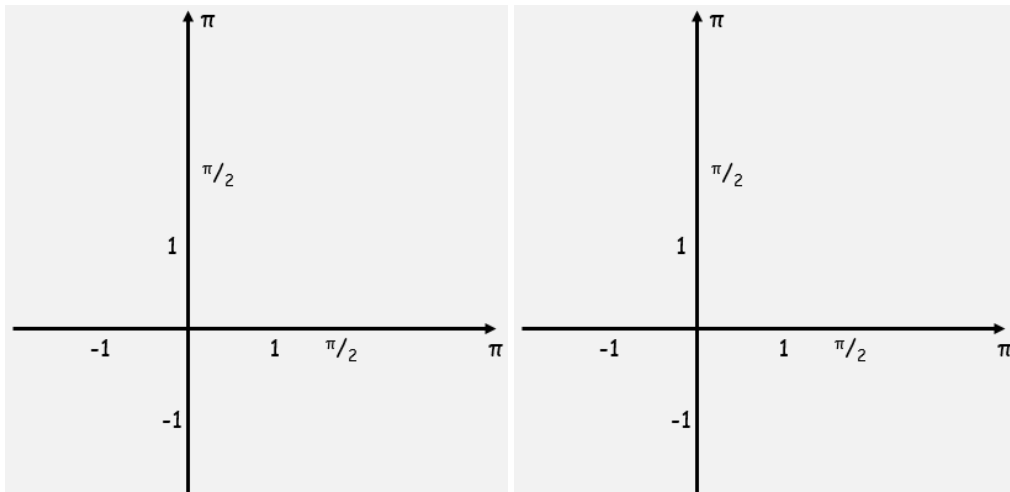
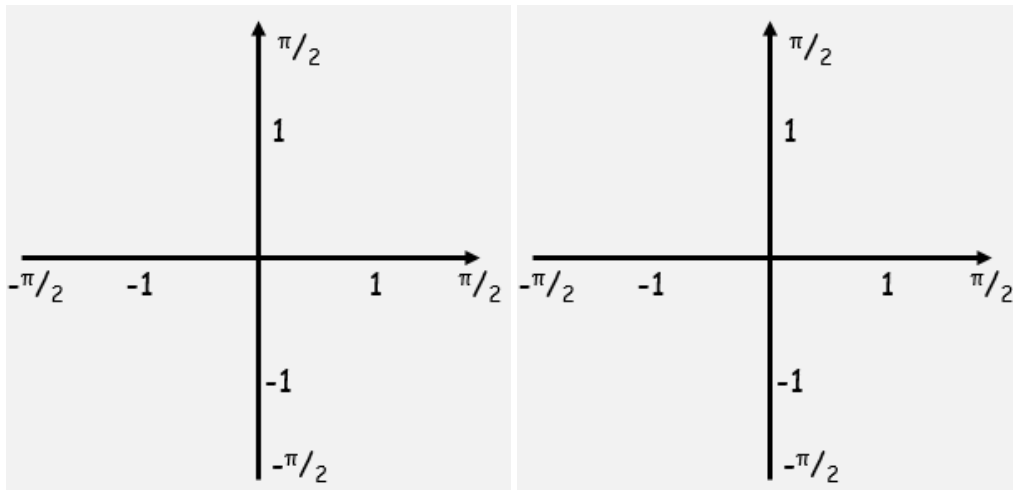
3. Solve the equation

$$4\operatorname{cosec}^2\theta - 9 \equiv \cot\theta$$

in the interval

$$0 \leq \theta \leq 360$$

6E Inverse Trigonometric Functions



1. Work out, in radians, the value of:

a) $\arcsin(0.5)$

b) $\arctan(\sqrt{3})$

c) $\arcsin\left(-\frac{\sqrt{2}}{2}\right)$

d) $\cos[\arcsin(-1)]$