## Chapter 5 - Statistics

## Probability Year 1

## Chapter Overview

## 1. Basic probability

2. Venn diagrams
3. Mutually Exclusive / Independent Events
4. Tree diagrams

| 3 | 3.1 | Understand and use <br> mutually exclusive and <br> independent events when <br> calculating probabilities. | Venn diagrams or tree diagrams may <br> be used. Set notation to describe events <br> may be used. <br> Use of $\mathrm{P}(B \mid A)=\mathrm{P}(B), \mathrm{P}(A \mid B)=\mathrm{P}(A)$, |
| :--- | :--- | :--- | :--- |
|  |  | Link to discrete and <br> continuous distributions. | $\mathrm{P}(A \cap B)=\mathrm{P}(A) \mathrm{P}(B)$ in connection with <br> independent events. <br> No formal knowledge of probability <br> density functions is required but <br> students should understand that area <br> under the curve represents <br> probability in the case of a continuous <br> distribution. |

(Set notation may be used in Year 1 - will be seen more commonly in Year 2)

## Probability concepts

An experiment is a repeatable process that gives rise a number a number of outcomes.

An event is a set of one or more of these outcomes.
(We often use capital letters to represent them)
$E=$ "rolling an even number"
$P=$ "rolling a prime number"

A sample space is the set of all possible outcomes.

Because we are dealing with sets, we can use a Venn diagram, where

- the numbers are the individual outcomes,
- the sample space is a rectangle and
- the events are sets, each a subset of the sample space.
You do not need to use set notation like $\cap$ and $U$ in this module (but ordinarily you would!)


## Example

Two fair spinners each have four sectors numbered 1 to 4. The two spinners are spun together and the sum of the numbers indicated on each spinner is recorded.
Find the probability of the spinners indicating a sum of
(a) exactly 5
(b) more than 5

## Another Example

The table shows the times taken, in minutes, for a group of students to complete a number puzzle.

| Time, $t$ (min) | $5 \leq t<7$ | $7 \leq t<9$ | $9 \leq t<11$ | $11 \leq t<13$ | $13 \leq t<15$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 6 | 13 | 12 | 5 | 4 |

A student is chosen at random. Find the probability for a group of students to complete a number puzzle
(a) In under 9 minutes (b) in over 10.5 minutes.

