## 1A Exponential Models

| $\boldsymbol{t}$ | 3 | 5 | 6 | 8 | 9 | 11 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{g}$ | 1.04 | 1.49 | 1.79 | 2.58 | 3.1 | 4.46 |

1. The table above shows some data collected on the temperature, in ${ }^{\circ} \mathrm{C}$, of a colony of bacteria ( t ), and its growth rate ( g ).

The data are coded using the changes of variable $x=t$ and $y=\log g$. The regression line of $y$ on $x$ is found to be:
$y=-0.2215+0.0792 x$
a) Mika says that the constant -0.2215 in the regression line means that the colony is shrinking when the temperature is $0^{\circ} \mathrm{C}$. Explain why Mika is wrong.
b) Given that the data can be modelled by an equation of the form $g=k b^{t}$, where $k$ and $b$ are constants, find the values of $k$ and $b$.

## 1B PMCC

| Day of <br> month | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $w$ | 4 | 4 | 8 | 7 | 12 | 12 | 3 | 4 | 7 | 10 |
| $g$ | 13 | 12 | 19 | 23 | 33 | 37 | 10 | n/a | n/a | 23 |

1. From the large data set, the daily mean windspeed, $w$ knots, and the daily maximum gust, $g$ knots, were recorded for the first 10 days in September in Hurn in 1987.
a) State the meaning of $n / a$ in the table
b) Calculate the product moment correlation coefficient for the remaining 8 days

c) With reference to your answer to part b), comment on the suitability of a linear regression model for this data

## 1C Hypothesis Testing for Correlation

1. A scientist takes 30 observations of the masses of two reactants in an experiment. She calculates a PMCC of $r=-0.45$.

The scientist believes there is no correlation between the masses of the two reactants. Test, at the $10 \%$ level of significance, the scientist's claim, stating your hypotheses clearly.

| Product Moment Coefficient |  |  |  |  | Sample <br> size, $n$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Level |  |  |  |  |  |
| 0.10 | 0.05 | 0.025 | 0.01 | 0.005 |  |
| 0.8000 | 0.9000 | 0.9500 | 0.9800 | 0.9900 | 4 |
| 0.6870 | 0.8054 | 0.8783 | 0.9343 | 0.9587 | 5 |
| 0.6084 | 0.7293 | 0.8114 | 0.8822 | 0.9172 | 6 |
| 0.5509 | 0.6694 | 0.7545 | 0.8329 | 0.8745 | 7 |
| 0.5067 | 0.6215 | 0.7067 | 0.7887 | 0.8343 | 8 |
| 0.4716 | 0.5822 | 0.6664 | 0.7498 | 0.7977 | 9 |
| 0.4428 | 0.5494 | 0.6319 | 0.7155 | 0.7646 | 10 |
| 0.4187 | 0.5214 | 0.6021 | 0.6851 | 0.7348 | 11 |
| 0.3981 | 0.4973 | 0.5760 | 0.6581 | 0.7079 | 12 |
| 0.3802 | 0.4762 | 0.5529 | 0.6339 | 0.6835 | 13 |
| 0.3646 | 0.4575 | 0.5324 | 0.6120 | 0.6614 | 14 |
| 0.3507 | 0.4409 | 0.5140 | 0.5923 | 0.6411 | 15 |
| 0.3383 | 0.4259 | 0.4973 | 0.5742 | 0.6226 | 16 |
| 0.3271 | 0.4124 | 0.4821 | 0.5577 | 0.6055 | 17 |
| 0.3170 | 0.4000 | 0.4683 | 0.5425 | 0.5897 | 18 |
| 0.3077 | 0.3887 | 0.4555 | 0.5285 | 0.5751 | 19 |
| 0.2992 | 0.3783 | 0.4438 | 0.5155 | 0.5614 | 20 |
| 0.2914 | 0.3687 | 0.4329 | 0.5034 | 0.5487 | 21 |
| 0.2841 | 0.3598 | 0.4227 | 0.4921 | 0.5368 | 22 |
| 0.2774 | 0.3515 | 0.4133 | 0.4815 | 0.5256 | 23 |
| 0.2711 | 0.3438 | 0.4044 | 0.4716 | 0.5151 | 24 |
| 0.2653 | 0.3365 | 0.3961 | 0.4622 | 0.5052 | 25 |
| 0.2598 | 0.3297 | 0.3882 | 0.4534 | 0.4958 | 26 |
| 0.2546 | 0.3233 | 0.3809 | 0.4451 | 0.4869 | 27 |
| 0.2497 | 0.3172 | 0.3739 | 0.4372 | 0.4785 | 28 |
| 0.2451 | 0.3115 | 0.3673 | 0.4297 | 0.4705 | 29 |
| 0.2407 | 0.3061 | 0.3610 | 0.4226 | 0.4629 | 30 |
| 0.2070 | 0.2638 | 0.3120 | 0.3665 | 0.4026 | 40 |
| 0.1843 | 0.2353 | 0.2787 | 0.3281 | 0.3610 | 50 |
| 0.1678 | 0.2144 | 0.2542 | 0.2997 | 0.3301 | 60 |
| 0.1550 | 0.1982 | 0.2352 | 0.2776 | 0.3060 | 70 |
| 0.1448 | 0.1852 | 0.2199 | 0.2597 | 0.2864 | 80 |
| 0.1364 | 0.1745 | 0.2072 | 0.2449 | 0.2702 | 90 |
| 0.1292 | 0.1654 | 0.1966 | 0.2324 | 0.2565 | 100 |


| $x$ | 31 | 28 | 38 | 37 | 18 | 17 | 21 | 29 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
| $y$ | 99 | 94 | 87 | 80 | 80 | 89 | 84 | 86 |

2. The table from the large data set shows the daily maximum gust, $x \mathrm{kn}$, and the daily maximum relative humidity, $y \%$, in Leeming for a sample of eight days in May 2015.
a) Find the PMCC for these data
b) Test, at the $10 \%$ level of significance, whether there is evidence of a positive correlation between daily maximum gust and daily maximum humidity. State your hypotheses clearly
