

Working with Vectors

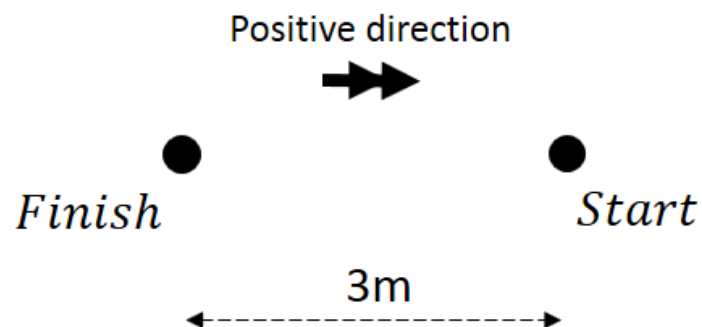
In Mechanics you will often need to convert to/from the scalar form of a quantity and the vector form.

SCALAR:
VECTOR:

Examples of scalars and vectors:

<u>Scalar</u>	<u>Vector</u>

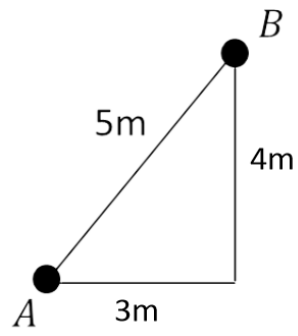
NB: 1-dimensional vectors are still different from scalars. Consider the displacement on a 1-dimensional line in a particular direction. If we'd gone backwards 3 units...



What is the distance travelled?

What is the displacement of the particle?

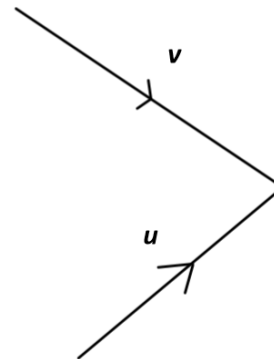
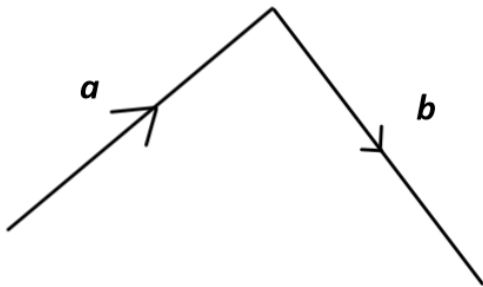
Vector Notation



Column Notation

***i-j* Notation**
(i and j are unit vectors of length 1)

Adding and Subtracting Vectors



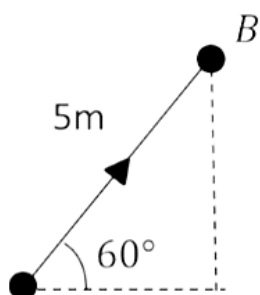
Two vectors are equal if they have the **same magnitude and direction**.

Two vectors are parallel if they have the **same direction but different magnitudes**.

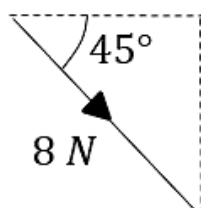
Converting Between Vectors and Scalars

To convert to vector form, just use basic trigonometry to find the x -change and y -change.

Scalar (Distance)



Vector (Displacement)



To convert scalar form, just find the **magnitude** of the vector using Pythagoras.

Vector (Velocity)

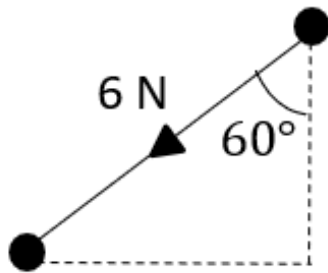
Scalar (Speed)

$$\begin{pmatrix} 5 \\ -12 \end{pmatrix} \text{ms}^{-1}$$

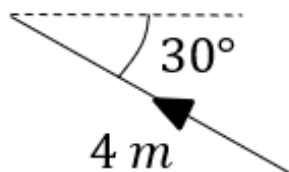
Further Examples

Scalar Form

Vector Form



$$(6\mathbf{i} - 8\mathbf{j}) \text{ ms}^{-2}$$



Test Your Understanding

A woman walks from A to B and then from B to C.

Her displacement from A to B is $6\mathbf{i} + 4\mathbf{j}$ m.

Her displacement from B to C is $5\mathbf{i} - 12\mathbf{j}$ m.

- a) What is the magnitude of the displacement from A to C?
- b) What is the total distance the woman has walked in getting from A to C?