

Logarithms

$\log_a n$ ("said log base a of n ") is equivalent to $a^x = n$.

The log function outputs the **missing power**.

Examples

$$\log_5 25 =$$

$$\log_3 81 =$$

$$\log_2 32 =$$

$$\log_{10} 1000 =$$

$$\log_4 1 =$$

$$\log_4 4 =$$

$$\log_2 \left(\frac{1}{2}\right) =$$

$$\log_3 \left(\frac{1}{27}\right) =$$

$$\log_2 \left(\frac{1}{16}\right) =$$

$$\log_a (a^3) =$$

$$\log_4 (-1) =$$

With your calculator...

$\log_{\square} \square$

$$\log_3 7 =$$

$$\log_5 0.3 =$$

\ln

$$\ln 10 =$$

$$\ln e =$$

\log

$$\log 100 =$$

Extension

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[MAT 2015 1J] Which is the largest of the following numbers?

- A) $\frac{\sqrt{7}}{2}$ B) $\frac{5}{4}$ C) $\frac{\sqrt{10!}}{3(6!)}$
D) $\frac{\log_2 30}{\log_3 85}$ E) $\frac{1+\sqrt{6}}{3}$

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[MAT 2013 1F] Three *positive* numbers a, b, c satisfy

$$\begin{aligned}\log_b a &= 2 \\ \log_b(c - 3) &= 3 \\ \log_a(c + 5) &= 2\end{aligned}$$

This information:

- A) specifies a uniquely;
- B) is satisfied by two values of a ;
- C) is satisfied by infinitely many values of a ;
- D) is contradictory