1. Static Rigid Bodies

Recall from the chapter on moments that for a stationary rigid body:

- The resultant force is 0.
- The resultant moment is 0.

The problems are the same as in the moments chapter, except now we may need to consider frictional forces.

Example

A uniform rod AB of mass 45kg and length 12m rests with the end A on rough horizontal ground. The rod rests against a smooth peg C where AC=8 m. The rod is in limiting equilibrium at an angle of 15° to the horizontal. Find:

- (a) the magnitude of the reaction of C
- (b) the coefficient of friction between the rod and the ground.

Example (EdExcel M2 Jan 2012 Q5)

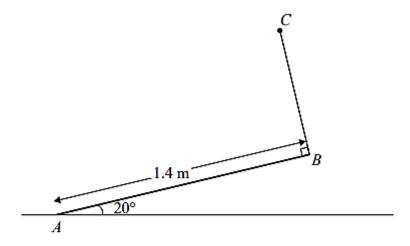


Figure 2

A uniform rod AB has mass 4 kg and length 1.4 m. The end A is resting on rough horizontal ground. A light string BC has one end attached to B and the other end attached to a fixed point C. The string is perpendicular to the rod and lies in the same vertical plane as the rod. The rod is in equilibrium, inclined at 20° to the ground, as shown in Figure 2.

(a) Find the tension in the string.

(4)

Given that the rod is about to slip,

(b) find the coefficient of friction between the rod and the ground.

(7)

Test Your Understanding (EdExcel M2 Jan 2013 Q3)

A ladder, of length 5 m and mass 18 kg, has one end A resting on rough horizontal ground and its other end B resting against a smooth vertical wall. The ladder lies in a vertical plane perpendicular to the wall and makes an angle α with the horizontal ground, where $\tan \alpha = \frac{4}{3}$, as shown in Figure 1. The coefficient of friction between the ladder and the ground is μ . A woman of mass 60 kg stands on the ladder at the point C, where AC = 3 m. The ladder is on the point of slipping. The ladder is modelled as a uniform rod and the woman as a particle.

Find the value of μ .

5 m C 3 m

Figure 1

(9)